## TEST AND EVALUATION OF ALUMINUM DRILL PIPE FOR DEEP WATER CORING

## DESIGN AND USE OF HEAVY WALL DRILLING JOINTS FOR BENDING STRESS REDUCTION



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## THE COVER PICTURE

The cover shows a horizontal heavy wall drilling joint in a test frame. The fixture applied tension loads of 400,000 pounds to the drilling joint while simultaneously bending the joint and connections to a $350-$ foot radius arc. Strain gages were attached to the tube wall and connection at critical points to measure stress levels. Test results proved the design acceptable for use at the critical upper end of the drill string.

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## PREFACE

Technical Report No. 15 includes two papers dealing with means of extending the drill string depth capability and lowering stresses at the top of the drill string.

The first paper titled "Test and Evaluation of Aluminum Drill Pipe for Deep Water Coring" reports on the operational use of a 2000 foot section of aluminum drill pipe in a mixed aluminum/steel drill string. The report also discusses metallurgical laboratory tests and assesses the potential of mixed strings for use in wireline coring operations to 30,000 feet.

The second technical study is entitled "Design and Use of Heavy Wall Drilling Joints for Bending Stress Reduction ". This report deals with the development and test of drilling joints used to reduce stresses at the upper end of the drill string. These stresses include static, dynamic, and bending loads. For very deep water coring operations or very slow penetration rates, 300 feet of the special joints are placed in the upper end of the drill string. The larger pipe cross-sectional area and the machined hubs design have allowed wireline coring operations to 23,000 feet with 5-inch drill pipe.

## ACKNOWLEDGEMENTS

The Deep Sea Drilling Project (DSDP) gratefully acknowledges the cooperation of the Reynolds Metals Company in the testing and evaluation of aluminum drill pipe (ADP) for deep ocean wireline coring. Reynolds personnel have periodically assisted in ADP inspection and have undertaken fatigue and metallurgical tests to aid in the Project's evaluation of ADP.

Analysis and operational test results indicate the feasibility of a 30,000 foot mixed aluminum-steel drill string design for wireline coring.

The report "Test and Evaluation of Aluminum Drill Pipe for Deep Water Coring" was prepared by Mr. Don Bellows, a mechanical engineer with DSDP's Development Engineering Department.

The report "Design and Use of Heavy Wall Drilling Joints for Bending Stress Reduction" was prepared by Mr. Stan Serocki, head of DSDP's Development Engineering Department.

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TEST AND EVALUATION OF ALUMINUM DRILL PIPE FOR DEEP WATER CORING

## CONTENTS

Page
SUMMARY ..... 1
INTRODUCTION ..... 1
ANALYSIS AND PROPOSED DESIGN ..... 1
COMPUTER MODEL ..... 3
OPERATIONAL TESTS ..... 4
INSPECTIONS ..... 5
LABORATORY/METALLURGICAL TESTS ..... 8
FATIGUE TESTS ..... 9
CONCLUSIONS AND RECOMMENDATIONS ..... 10

## LIST OF FIGURES

Page

1. Guide Shoe and Picalo System ..... 15
2. Aluminum Drill Pipe ..... 16
3. Configuration of $30,000-$ Foot Drill String ..... 17
4. Computer Setup for 30,000-Foot Drill String ..... 18
5. Half Amplitude of Displacement of Drill String ..... 19
6. Half Amplitude of Velocity of Drill String ..... 20
7. Dynamic Stress in Drill String ..... 21
8. Total Stress in Drill String ..... 22
9. Fatigue Life of Drill String ..... 23
10. Transfer Function of Dynamic Loading of Drill String ..... 24
11. Exfoliation of Aluminum Drill Pipe ..... 25
12. Intergranular Attack ..... 25
13. Recrystallized Layer ..... 26
14. Fatigue Curve for 2014-T6 Aluminum Alloy ..... 26
LIST OF TABLES
I. Results of Fatigue Tests ..... 27
II. Aluminum Drill Pipe Usage on Deep Sea Drilling Project ..... 28
III. Chronological History of ADP Used by DSDP ..... 29

Analysis and operational testing show that aluminum drill pipe (ADP) can be used to extend deep ocean coring limits from 23,000 feet to 30,000 feet. The mixed aluminum-steel drill string design maintains a 4-inch drift diameter which is highly desirable for continuous wireline coring. Alternate all steel designs require tapered strings with reduced drift diameters. Fatigue and corrosion characteristics of ADP are evaluated and found to be acceptable for deep water wireline coring operations.

## INTRODUCTION

The Deep Sea Drilling Project (DSDP) coring program started in 1968 as part of the Ocean Sediment Program funded by the National Science Foundation (NSF). Wireline coring is limited to about 23,000 feet by the present drill string design which is 5-inch diameter, 19.5 pounds per foot, $\mathrm{S}-135$ steel. The string is not tapered and therefore maintains a constant 4-inch drift bore for efficient wireline coring operations.

Ultra-deep scientific objectives require a 30,000-foot drill string capability, preferably with a 4-inch drift bore. Such a requirement limits the use of conventional steel tapered drill strings as a practical option for a 4-inch bore. This study examines a mixed steel aluminum design which can meet the desired scientific criteria and maintain reasonable stress levels at the upper end of the drill string. The report includes a performance analysis of the mixed string including load and length limitations, resonance considerations, and an evaluation of fatigue life and corrosion. The results of laboratory metallurgical tests and operational tests are discussed.

## ANALYSIS AND PROPOSED DESIGN

It has been recognized since the beginning of the Deep Sea Drilling Project that the standard 5 -inch, 19.5 pound, $S-135$ steel drill pipe would limit drill string length to about 20,000 feet. Actually, string lengths of 23,000 feet have been deployed, but special precautions were taken such as using a picalo to reduce bending stresses in the moon pool, using new pipe at the top of the string, and operating in calm seas. The moon pool is the well immediately below the rig floor which is open to the sea and through which the drill string is deployed. The ship has a built-in horn shaped guide shoe in the moon pool which insures that the drill pipe is bent uniformly and gradually during pitch and roll motions and is not bent sharply around any edges. The radius of the guide shoe is 350 feet. Under high loading conditions a picalo is sometimes used. It is a section of tapered pipe that is used in the guide shoe and which restricts the radius of curvature of the drill pipe passing through it to about 450 feet, thereby decreasing the bending stress. The guide shoe
and picalo are shown in Figure 1. Even under the special conditions noted above, the 23,000 -foot string of 5 -inch pipe is used at 90 to 95 percent of the yield strength.

Various options are available to permit the use of long drill strings:

1. Tapered drill string using larger diameter pipe at top of string.
2. "Tapered" drill string using same outer diameter pipe throughout but with greater wall thickness at top of string.
3. Mixed drill string using pipe of different materials, e.g., steel and aluminum.

Options 1) and 2), which were analyzed in the Mohole Report (Reference 1), have some inherent practical difficulties such as non-standard sizes, distinguishing among the various sizes and wall thicknesses in operational use, and maintaining a 4-inch drift bore for efficient coring with the present hardware. A concentrated analytical effort has been devoted to the mixed drill string using steel and ADP. An investigation was conducted as to the technical feasibility of using 5-inch ADP in conjunction with the 5-inch steel pipe already in use on the ship GLOMAR CHALLENGER. The items considered in this investigation were strength, fatigue life, static and dynamic loading, resonance, corrosion, shipboard handling, quality control at the manufacturer's extrusion plant, and in-service experience by various oil companies. It should be noted that mixed strings are not a new innovation; they have been used by many drilling companies (Reference 2). The unique aspect of this investigation is the configuration of a 30,000 -foot mixed drill string while maintaining the 4 -inch bore.

The ADP is manufactured by Reynolds Metals Company (RMC). Some pertinent characteristics of the pipe are (See Figure 2):

> Length of joint (ft. nominal)................ 30
> Outer diameter of body of pipe (in)......... 5.150
> Wall thickness of body of pipe (in)......... 0.525
> Weight per foot in seawater (lbs)........... 9.2
> Diameter of tool joint (in).................... 7.0
> Minimum yield strength (psi)................... 58,000

The aluminum is type 2014-T6. The inside diameter of the pipe is constant at 4.1 inches. The outside has a 41-46 inch long tapered transition at each end which brings the outer diameter from 5.150 inches on the body to 5.688 inches at the tool joint. The in-water weight of 9.2 pounds per foot compares with 18.8 pounds per foot for 5-inch steel pipe. More details on dimensions and weights for the ADP can be found in Reference 3.

The configuration of a $30,000-$ foot mixed drill string would be 5,000 feet of 5 -inch steel pipe at the bottom, then 10,000 feet of 5 -inch ADP, 10,000 feet of 5 -inch steel, and finally 5,000 feet of 5.5 inch steel pipe. This represents a slight tapering of this mixed string. However, the 4 -inch minimum bore is still maintained. (This configuration is shown schematically in Figure 3). The 5,000 feet of steel pipe at the bottom of the string is used so that the ADP does not enter the hole and become abraded in chert or basaltic intervals. Reynolds has specified that mixed strings of steel and aluminum should include at least 5 percent aluminum, which condition is obviously satisfied. The objective of the configuration described is to use each of the major sections of the string to its full capability which has been set at 90 percent of the yield strength to allow a ten percent margin for safety.

Fatigue life is also an important consideration when working from a. drilling ship. Two types of dynamic stress and the resultant effect on the fatigue life of drill string material must be monitored. Axial dynamic stress results from the heave motion of the ship, and bending dynamic stress is caused by the pitch or roll of the ship. The axial dynamic stress is present during the total time that the string is deployed, but decreases in magnitude lower in the string. The bending dynamic stress is present only in that section of pipe which is passing through the guide shoe. Once a particular length of pipe has been lowered beneath the keel, the bending stress is no longer present. Therefore, it is desirable, when drilling, that the rate of penetration be such that one section of pipe is not subjected to long intervals of bending in the guide shoe.

## COMPUTER MODEL

DSDP has developed a computer model of the drill string which predicts stresses, displacements, and fatigue life for any element along the length of the drill string. Figures 4 through 10 represent a run of the computer program for the 30,000-foot mixed string configuration discussed previously. Figure 4 lists the setup data that is interactively entered into the computer. It shows no heave compensation, velocity dependent hydrodynamic damping, and a Pierson-Moskowitz sea spectrum. Figure 5 shows the amplitude of displacement along the string with wave height as the curve index. Figure 6 shows the velocity along the string. The top displacement and velocity is the heave motion of the ship, and it can be seen from Figures 5 and 6 that the displacement and velocity at the bottom of the string are greater than at the top. This is due to the elastic properties of the string and the resultant stretching. Figure 7 shows the dynamic axial stress in any element of the string. This stress is caused by the heave motion of the ship. Figure 8 shows the total stress which is the sum of the static stress and the dyanmic stress. The static stress is the in-water weight of the portion of the string below the element being considered. Figure 9 shows the
fatigue life and indicates that the ADP fatigue life is approximately 1000 hours in this configuration. The computer fatigue life estimate of 1000 hours for a $30,000-$ foot string appears to be too low based on Project experience. The fatigue prediction algorithm and the fitting of the fatigue curve are being reviewed for range of applicability. Figure 10 shows the resonance condition for the string. The fundamental resonant period is about 3.3 seconds which is in the low energy portion of the ocean wave spectrum, and therefore the string is not likely to be excited to resonance. It should be noted that the computer model, in its present form, calculates only the static and dynamic stress. The bending stress, as the pipe passes through the guide shoe, must also be taken into account and added to the static and dynamic stress. For the 30,000-foot configuration, the total stress leaves a calculated margin which is adequate for an overpull of only 50,000 pounds in the event of a stuck pipe.

## OPERATIONAL TESTS

An operational test of the ADP was necessary in order to fully evaluate its suitability in long drill strings. Various aspects of operational use were to be considered including fatigue life, coatings and their effect on corrosion, handling, and inspection methods. An order was initiated with Reynolds Metals Company, the only supplier of ADP, and in November 1978, the first shipment of 42 joints of 5 -inch ADP was put aboard the ship. Shortly thereafter 21 additional joints were delivered to make a total of 63 joints (approximately 1900 feet). The 63 joints were all shot peened on the interior but had various interior coatings--21 joints were coated with Drilcote, a Reynolds proprietary epoxy coating; 21 joints were coated with Dimetcote, an inorganic zinc coating produced by Ameron; and 21 joints were left without any coating. The 21 joints that were coated internally with Dimetcote were also coated externally with the same coating. The ADP was to be put in service for about 12 to 18 months; then an evaluation was to be conducted and the pipe was to be taken off the ship. However, after the initial trial period, more exposure was needed for evaluation and the pipe was left on board. As of the date of this report, the original order of ADP has been on the ship for about five years.

The ADP has a number of advantages over steel pipe, the most significant of which is weight. The 5-inch ADP weighs only half as much as the standard 5 -inch steel pipe that has been used on the ship. Another distinct advantage is the lower Young's modulus of aluminum-one third that of steel. This allows the ADP to bend in a tighter arc with less stress being developed which is an important consideration when the pipe is being lowered through the guide shoe in the moon pool. Also, the ADP has better low temperature toughness and higher fatigue endurance than steel pipe. Because of the lighter weight and lower Young's modulus of the ADP, it can be rotated at higher speed before encountering critical vibrations. The price per foot of ADP is comparable to
that of the steel pipe.
The operational tests have shown that there are no operational problems in handling the ADP. The pipe is made up into stands-three joints coupled together--for a total length of 90 feet. These stands are then laid horizontally in a mechanized pipe racker. Each stand must be drawn from the horizontal position to a vertical position. The bending experienced by the ADP during this process is well within the capability of the pipe. Because of extreme drill string lengths and the possibility of pipe damage caused by slips, elevators rather than slips are used with all pipe. The aluminum pipe is handled with a special 5-1/2 inch, 18 degree taper elevator modified to handle the 5.688 inch diameter below the box tool joint.

## INSPECTIONS

As the performance of the ADP was of mutual interest to DSDP and Reynolds, both parties have participated in frequent inspections of the pipe. In January, 1979, Reynolds inspected the ADP. Approximately 39 joints were visually examined. Four joints were inspected by internal borescope and by ultrasonic wall thickness gaging. The borescope is an optical device which can be passed through the bore of the pipe and which enables the user to see the condition of the interior of the pipe. The borescope inspection was performed on two joints coated on the inside with Drilcote and two joints that were bare on the inside. No corrosion was observed in the coated joints. Profuse, broad but shallow pitting was observed in the two bare joints. This type of corrosion is normal for the 2014 alloy in a marine environment. The external surface of all the ADP displayed profuse shallow pitting which again is normal for 2014. Normal, light galvanic pitting was observed on the pipe surfaces next to the steel tool joints. Measured pits were less than .005 inch deep. The ultrasonic thickness gaging showed the thickness exceeding the . 525 inch specified nominal thickness for new pipe. After inspection, all of the ADP was found suitable for further service.

In 1980, another inspection was performed at the Norfolk, Virginia port call by personnel from Reynolds, Richmond. Visual inspection was made on the complete test string of ADP. Corrosion and fatigue were evaluated and the wall thickness was measured using a Sonotest Model UTG-5 ultrasonic thickness gage. The ADP test string was considered to be in satisfactory condition and was put back in service.

Unlike conventional drill pipe which can become thin anywhere along the length, experience has shown that ADP will always exhibit its minimum wall at the mid-point of the length. It has never been found otherwise. This characteristic permits inspection of ADP at the rig site to determine the minimum remaining wall at the mid-length of each joint. Pi tapes (furnished by Reynolds) are used initially around the circumference at the mid-
length to determine the diameter. This value, as related to the original diameter, then indicates remaining wall assuming that all wear has occurred on the outside and that the bore is free of major corrosion which can be checked with a borescope. This system is satisfactory if no more than . 200 inch is missing from the O.D. at the mid-length. If O.D. loss at the mid-length exceeds .200 inch, then an ultrasonic wall thickness gage must be used.

In the fall of 1981, Reynolds requested Tuboscope to make an evaluation of the Drilcote coating that was applied to some of the ADP. Tuboscope found the coating to be generally intact and in good condition. Small patches of coating had been removed and these areas were associated with grooves or cuts in the surface of the coating. The cuts were usually long and were deduced to be caused by running the wireline for core retrieval.

In November 1981, a complete inspection of the ADP was performed jointly by DSDP and Reynolds at the Panama port call. The inspection consisted of:

1) Visual inspection of exterior and interior.
2) Measured depth of typical "deepest" pits on exterior.
3) Measured length - if not stretched, length should be 30 feet, plus 2 inches, minus 0 .
4) Measured wall thickness.

The type of coating on the interior of the pipe could be determined visually. The Drilcote had a greenish cast and was very smooth and reflective. The uncoated interior had a dark, but smooth and reflective appearance. The Dimetcote (zinc) coating had a rough, pitted, non-reflective appearance. The wall thickness was measured with a Nova 201 Ultrasonic Thickness gage made by NDT Instruments of Huntington Beach, CA. The gage was calibrated on a single ring cross section of pipe before and after each set of measurements. The results of this inspection were:
1). Most of the pipe showed general pitting (about . 025 inch deep maximum) on the exterior although some joints were relatively free from pitting.
2) Five joints exhibited severe exfoliation, i.e., large patches of 3 to 4 square inches each, usually on the tapered region at the pin end. It should be noted that severe does not mean deep since, even in the exfoliated areas, the wall thickness was greater than that specified for new pipe.
3) The smoothest, least corroded interiors were those coated with Drilcote. The bare interior was the next best. The pipe coated on the interior with Dimetcote
(zinc) had general pitting throughout the interior.
4) No stretching was observed on any of the joints.
5) All of the wall thickness measurements were greater than that specified for new pipe (. 525 inch). This was true even for the exfoliated regions.

Twenty four joints exhibited some exfoliation ranging from minor to severe. The five joints with severe exfoliation were pulled out and shipped to Houston to be shot peened on the exterior. The remaining joints of ADP were declared suitable for continued service. This was to have been a test to determine if shot peening would decrease the exfoliation. However, all of the exfoliation was not removed by the shot peening so it was not a valid test. The shot peening would have to be done on new pipe to provide a proper test. A detailed investigation of the exfoliation problem was conducted and this is discussed in the next section.

The most recent inspection of the ADP was again a joint effort with Reynolds and DSDP and was held at the port call in Norfolk, Virginia in June 1983. The inspection consisted of:

1) Visual examination of the exterior.
2) Check of I.D. numbers to locate ten new joints that were shot peened on the exterior and delivered to the ship in September 1982.
3) Ultrasonic wall thickness measurements.
4) Borescope examination of interior of pipe.
5) Scrapings from interior of pipe to test for zinc coating.

The results of the inspection were:

1) The exterior condition of the pipe was about the same as in the 1981 inspection.
2) All of the wall thickness measurements were greater than that specified for new pipe (. 525 inch).
3) Most of the pipe showed smooth reflective interiors. The non-reflective pitted interiors were examined more closely with the borescope and the pits were found to be very shallow.
4) There was no exfoliation on the ten new joints. There were some corrosion blisters and light galvanic corrosion on the aluminum adjacent to the steel tool joints.

Three joints of pipe were pulled out at this inspection and
shipped to the Reynolds, Richmond facility for testing. Two of these joints had severe (as previously defined) exfoliation and will be put in the rotating beam fatigue test machine. The third joint was observed spraying water from the tool joint when the stands of pipe were being broken into singles after the previous deployment. This tool joint will be cut open to examine the interior for some feature that may have caused the entrapment of water under pressure. The scrapings from the inside of the pipe have been analyzed but they do not show anything conclusive as to the effect of the zinc coating on the interior condition of the pipe.

## LABORATORY/METALLURGICAL TESTS

In the summer of 1981, exfoliation of the exterior of the ADP was detected, and in some cases, it appeared to be rather severe. One joint with extensive exfoliation was taken off the ship and sent to the Reynolds, Richmond facility for fatigue testing. Figure 11 shows a typical case of exfoliation.

Visual examination of the complete drill pipe joint showed that the exfoliation was much more severe at the ends of the pipe. On peeling back some of the surface, there was clear indication of corrosion product. Since the amount and extent of corrosion attack was observed to vary from one end of the pipe to the other, it seemed advisable to examine the depth and type of corrosion attack, as well as the thickness of the recrystallized layer along the length of the pipe. One-inch thick rings were cut at $1^{\prime \prime}, 4^{\prime \prime}, 4^{\prime \prime}, 4^{\prime \prime}, 60^{\prime \prime}$, and $8^{\prime \prime}$, from the pin end of the pipe. These samples were etched in caustic to reveal the grain structure. The recrystallized layer on the exterior surface varied from very light (0.020") in the heavy wall to substantial ( $0.120^{\prime \prime}$ to $0.130^{\prime \prime}$ ) at the $80^{\prime \prime}$ section. The interior surface also showed a recrystallized layer, which was much thinner and uniform along the $80^{\prime \prime}$. length examined. Figure 13 shows that a recrystallized layer exists at both the inside and outside surface of the pipe.

As with the pin end, one inch rings were cut and machined at $10^{\prime \prime}$, 41", 43", 46", 60", and 80", from the box end of the pipe. These samples were etched in caustic to reveal the grain structure. There was no discernible recrystallized structure at the $10^{\prime \prime}$, 41", 43", and 46" locations, while the $60^{\prime \prime}$ section had a recrystallized skin of >0.125".

Intergranular corrosion was seen in many of the box-end and pinend cross-sections, with the depth of attack generally on the order of $0.020^{\prime \prime}$ or less. One extreme example of intergranular attack is shown in Figure 12, where the attack has penetrated to a depth of $0.044^{\prime \prime}$. A larger view of this same section of the pipe is shown in Figure 13, where the total depth of the recrystallized layer is $0.130^{\prime \prime}$.

The reason for the noted exfoliation and intergranular corrosion is not clear at this time, but improved heat treating practice is expected to prevent this from occurring in the future.

## FATIGUE TESTS

In the Spring of 1981, after 18 months of service, six joints of the ADP were taken off the ship and sent to the Reynolds, Richmond facility for fatigue testing. The six joints were chosen so that, on the interior surface, two were bare, two were Drilcote, and two were Dimetcote. Tests were conducted using a rotating cantilever beam fatigue machine. The speed of rotation was controlled at 300 rpm . The bending load was applied at the end of the test specimen, resulting in a moment arm to the end of the tool joint of approximately 109 inches. Two bending loads were employed:

200,000 in-lbs (max bending stress in body of pipe $=15,000$ psi)

170,000 in-lbs (max bending stress in body of pipe $=13,000$ psi)

The higher bending moment was included to provide a comparison with rotating beam tests previously performed on new, unused 5inch ADP. The lower bending moment was chosen to be equivalent to a 85 percent reduction factor to accommodate to the stress risers on the surface of the used pipe that result from abrasion, wear, and corrosion. The results of the fatigue tests are shown in Table I. As might be expected in fatigue testing, there was some scatter in the data especially for the case of new pipe where the cycles-to-failure ranged from $2.44 \times 10^{5}$ to $2.60 \times 10^{6}$. The most important observations on the used ADP were:

1) The failures occurred outside of the tool joints.
2) All fatigue failures occurred at visible stress risers.

Figure 14 shows a fatigue curve for sharply notched, round specimens of the ADP alloy 2014-T6 (Reference 4). The results of the fatigue tests from Table I have been over- plotted on the curve of Figure 14 and show very good agreement with the curve. It appears that sharply notched specimens are representative of the condition of used pipe that has been gouged and abraded during service, and therefore, contains stress risers comparable to the notches on the specimens. There is no endurance limit for nonferrous metals--the fatigue curve continues to decline at lower stress levels regardless of whether the surrounding medium is air or water.

The test results of Table $I$ are based upon the six joints of ADP that were chosen such that two joints were bare, two were coated
with Dimetcote, and two were coated with Drilcote. Another joint of ADP, which was severely exfoliated, was also sent to Reynolds for fatigue testing to see if the exfoliation had any effect on the fatigue life. The joint was tested at a stress level of 13,000 psi and it failed at 308,000 cycles. This fits in with the results of Table $I$, but the more important observation is that the failure did not occur in the exfoliated area. It seems, from this one test, at least, that the exfoliation does not produce stress risers that would lead to the start of fatigue cracks.

In addition to the fatigue testing, full sections of the used 5inch ADP were tensile tested using equipment at the Phoenix extrusion plant. All of the pipe exhibited tensile strengths in excess of the 488,000-pound value specified for new pipe.

Table II is a listing of the ADP usage by DSDP. At the stress levels ( $<8,000 \mathrm{psi}$ ) encountered during operations up to the present, it is estimated that about five percent of the fatigue life of the ADP has been consumed.

Table III is a chronological listing of the major events concerning the aluminum drill pipe during the 5-year period of usage by the DSDP.

## CONCLUSIONS AND RECOMMENDATIONS

From the results of the inspections and testing as described previously, the following conclusions may be drawn concerning the ADP that has been in service for five years in the Deep Sea Drilling Project:

1) The bare, shot peened interior seems to be holding up as well as the interior coated with Drilcote. The Dimetcote appears to be the least suitable.
2) The exfoliation, although cosmetically unattractive, does not appear to affect the fatigue life.
3) The recrystallization of the exterior surface of the pipe can not be eliminated, but may be mitigated with further metallurgical modifications.
4) Every joint of the ADP, on all inspections, has shown a wall thickness at mid-length greater than that specified for new pipe.
5) A very small percentage (5\%) of the fatigue life of the ADP has been consumed.
6) With the modified 5-1/2 inch, 18 degree elevators, handling of the ADP has presented no problems for the drilling crew.

The following recommendations are put forth for any future purchases and use of ADP:

1) Shot peen interior of pipe. Care must be exercised during this process; too much shot peening can cause the surface to become brittle and increase the chances of development of fatigue cracks.
2) For deep sea drilling applications, the pipe interior should be left bare.
3) Conduct scheduled inspections at approximate yearly intervals. Inspection should consist of:
a) Visual: exfoliation, pitting, gouges, cracks on exterior.
b) Borescope examination of interior for pitting or cracks.
c) Wall thickness measurements with ultrasonic gage.
d) Examination of tool joint threads as with steel pipe.
e) Length measurement to determine stretching.
4) Maintain a usage record so as to have a running account of fatigue life consumed.
5) Set limits on wall thickness and fatigue life and remove from service those joints of pipe which exceed the limits.

In general, DSDP has received good service from the test section of 5 -inch aluminum drill pipe, and based upon the computer work discussed previously, a mixed string of steel and ADP should be a viable option for reaching total depths of 30,000 feet while maintaining a 4 -inch drift bore.

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FIGURE 1


ALUMINUM DRILL PIPE
FIGURE 2 -16-


FIGURE 3

```
            RUN ID# 1368
\begin{tabular}{|c|c|c|c|c|}
\hline GROUP & LENGTH (FT) & \#ELEMENTS & RUBBER SPACING (FT) & PIPE TYPE \\
\hline 1 & 5000.0 & 10 & 7.0 & \(10=5.50 \mathrm{ST}\). API \\
\hline 2 & 5000.0 & 10 & 7.0 & \(1=5 \mathrm{ST}, \mathrm{P}\) PREM API \\
\hline 3 & 5000.0 & 10 & 7.0 & 1=5 ST., PREM API \\
\hline 4 & 5000.0 & 10 & 7.0 & 2=ALUMINUM, NEW \\
\hline 5 & 5000.0 & 10 & 7.0 & 2=ALUMINUM, NEW \\
\hline 6 & 5000.0 & 10 & 7.0 & \(4=5 \mathrm{ST}\). 90\%-WL API \\
\hline
\end{tabular}


HoC. DAMPING \(=2100 \quad\) BOT ASSY \(4 T=40000\)
DS END ATTACH =FREELY SUSPENDED INPUT LOCTN \(=T 0\) SHIP
SIG LAVVE HT \(=6\)
SHIP X-FCN \(=45\) OFF BOW PIERSON/MOSKOWITZ. \#ELT GR-S = 6
\(=0\)
0
BOT-GRND SPRING RATE \(=0\)
RDDED BOTTOM MASS \(=0\)
\(=0\)
```

| X-AXIS: ELEMENT DEPTH (FT) FROM | 0.00 TO | 0.00 BY | 0.00 |  |  |  |
| :--- | :--- | :--- | :--- | ---: | ---: | ---: | ---: |
| CUAVE INDEX: LAVE HEIGHT (FT) | VALUES | 6.00 | 9.00 | 12.00 | 15.00 | 18.00 |

PLOT \# 1: AMPLITUDE (FT) [1]
PLOT \# 3: DYNAMIC STRESS (LB/SQIN) [3]
PLOT \# 4: FATIGUE LIFE (LOG HRS) [4]
PLOT \# S: TOTAL STRESS (LB/SQIN) [5]

```

COMPUTER SETUP FOR \(\mathbf{3 0 , 0 0 0}\) FT DRILL STRING FIGURE 4








EXFOLATION OF ALUMINUM DRILL PIPE
FIGURE 11


INTERGRANULAR ATTACK
FIGURE 12

\section*{EXTERIOR SURFACE OF PIPE}


FIGURE 13


FATIGUE CURVE FOR 2014-T6 ALUMINUM ALLOY
FIGURE 14

TABLE I

RESULTS OF FATIGUE TESTS
\begin{tabular}{|c|c|c|c|}
\hline \[
\begin{aligned}
& \text { Description of } \\
& 5^{\prime \prime} \text { ADP Samples }
\end{aligned}
\] & \[
\frac{\text { Bending }}{\frac{\text { Moment }}{\text { In/Lbs }}}
\] & \[
\frac{\text { Cycles to }}{\text { Failure }}
\] & Remarks \\
\hline New & 200,000 & \[
\begin{aligned}
& 2.44 \times 10^{5} \text { to } \\
& 2.60 \times 10^{6}
\end{aligned}
\] & Failures occurred in transition zone near body of pipe \\
\hline Dimetcote & 200,000 & 117,400 & Broke 25-1/2" from tool joint at stress riser caused by 3 pitted spots on outer surface \\
\hline Drilcote & 200,000 & 175,600 & Broke 26" from tool joint at stress riser caused by one pit on outer surface \\
\hline No coating & 170,000 & 360,900 & Broke 3-1/2" from tool joint in transition zone. Stress risers at 2 pitted areas on outer surface \\
\hline Drilcote & 170,000 & 500,000* & No failure; stopped test \\
\hline Dimetcote & 170,000 & 454,700 & Broke 32" from tool joint at stress riser from one pitted spot on outer surface \\
\hline
\end{tabular}

TABLE II
ALUMINUM DRILL PIPE USAGE ON DEEP SEA DRILLING PROJECT
\begin{tabular}{|l|c|c|c|c|c|}
\hline LEG & DATE & \begin{tabular}{c} 
WATER \\
DEPTH \\
(M)
\end{tabular} & \begin{tabular}{c} 
LENGTH \\
OF ADP \\
(M)
\end{tabular} & \begin{tabular}{c} 
HOURS \\
ROTATING
\end{tabular} & \begin{tabular}{c} 
HOURS (1) \\
IN WATER
\end{tabular} \\
\hline 63 & Nov 78 & 3850 & 375 & 117 & 277 \\
66 & Apr 79 & 2850 & 375 & 161 & 224 \\
67 & May 79 & 2350 & 375 & 21 & 147 \\
73 & May 80 & 4800 & 567 & 72 & 711 \\
79 & May 81 & 4000 & 439 & 150 & 354 \\
80 & Jun 81 & 1250 & 448 & 13 & 82 \\
84 & Feb 82 & 3850 & 402 & 89 & 205 \\
85 & Apr 82 & 3900 & 439 & 40 & 72 \\
93 & May 83 & 4650 & 540 & 110 & 270 \\
95 & Sep 83 & 4650 & 503 & 150 & 339 \\
\hline & & & TOTALS & 923 & 2681 \\
\hline
\end{tabular}
(1) Drill string is not rotated during periods of wireline core retrieval.

\section*{CHRONOLOGICAL HISTORY OF ADP USED BY DSDP}
\begin{tabular}{|c|c|}
\hline Date & Event \\
\hline Nov 1978 & Received 42 joints (21 coated internally with Drilcote, 21 uncoated) \\
\hline Jan 1979 & Inspection of ADP on board ship in California by RMC \\
\hline Nov 1979 & Received 21 joints (coated internally and externally with Dimetcote) \\
\hline Sep 1980 & Pipe unloaded at Norfolk, VA and shipped to Bellwood, VA for inspection by RMC \\
\hline Feb 1981 & Six joints shipped to Richmond, VA for fatigue testing by RMC \\
\hline Apr 1981 & Exfoliated joint shipped from Europe to Richmond, VA for examination by RMC \\
\hline Sep 1981 & Evaluation of Drilcote coating by AMF/Tuboscope \\
\hline Nov 1981 & Inspection of ADP in Panama by DSDP and RMC \\
\hline Mar 1982 & Five joints shot peened and put back on ship \\
\hline Jun 1982 & Ten new joints received \\
\hline Jun 1983 & Inspection of 59 joints at Norfolk, VA by DSDP and RMC. Three joints shipped to Richmond, VA for testing and examination \\
\hline
\end{tabular}

\title{
DESIGN AND USE OF HEAVY WALL DRILLING JOINTS FOR BENDING STRESS REDUCTION
}

\section*{CONTENTS}
Page
SUMMARY ..... 35
INTRODUCTION ..... 35
TUBE DESIGN ..... 36
CONNECTION DESIGN ..... 38
TEST PROGRAM ..... 39
OPERATIONAL USE ..... 40
APPENDICES
I. SPECIAL HEAVY WALL DRILL PIPE FOR THE DEEP SEA DRILLING PROJECT ..... 49
II. FABRICATION DRAWING AND SPECIFICATION FOR HEAVY WALL DRILLING JOINT ..... 72
III. EXPERIMENTAL EVALUATION OF OPTIMUM 5-1.2" I.F. CONNECTION DESIGN ..... 79
IV. CALCULATED STRAINS AND DEFLECTIONS OF DRILLING SUBS COMPARED TO EXPERIMENTAL MEASUREMENTS ..... 137
LIST OF FIGURES
1. DRILL STRING IN GUIDE SHOE ..... 45
2. DEPENDENCY OF BENDING STRESS ON RUBBER SPACING ..... 46
3. HEAVY WALL DRILLING JOINT GUIDE ..... 47

This paper describes the design, test, and operational use of special heavy wall drilling joints. The drilling joints were developed for riserless coring and drilling, in water depths to 23,000 feet, carried out from the research vessel GLOMAR CHALLENGER. The drilling joints are designed for improved fatigue resistance at the upper end of the drill string which is exposed to reversed bending fatigue as the drill pipe rotates through a 350 -foot radius ( 16 degrees per 100 feet curvature) bending restraint. Full scale proof test of a pipe section demonstrated that the shoulders of the connection did not separate under a combined load of 402,000 pounds axial and a bending moment sufficient to deflect the pipe to 16 degrees per 100 feet. Heavy wall drilling joints have been in routine use since early 1978.

\section*{INTRODUCTION}

Deep Sea Drilling operations require significant penetration of basaltic basement rock. The maximum length of drill strings have reached 23,000 feet. A major source of fatigue is cyclic stresses generated as the drill pipe rotates in a bending restraint or guide shoe (see Figure 1). This guide shoe has been fitted between the rotary table and the keel of the vessel to restrain bending of the drill string. The shoe has a radius of curvature of 350 feet to 8 degrees maximum roll angle (half amplitude). Penetration rates in basalt are slow-on the order of 6 feet per hour in hard basalt. This slow rate of penetration through the guide shoe at high tensile loads can lead to early fatigue failure of the upper portion of the drill string with the present 5-inch, S-135, nominal 19.5 lbs/ft drill pipe.

The bending stresses generated are also a function of tension and the distance beteween supporting tool joints or drill pipe rubbers (Ref. 1). These bending stresses increase with increased tension and with increased length between supporting tool joints or rubbers. Figure 1 shows how the bending of the drill pipe is affected by this spacing. For Deep Sea Drilling operations the drill pipe is fitted with rubbers at an average spacing of 7 feet to reduce bending stresses. The effect of tension and rubber spacing is shown in Figure 2. At a top tension of \(410,000 \mathrm{lbs}\). for a 20,000-foot drill string, Figure 2 shows the bending stress can vary from \(22,000 \mathrm{psi}\) for a 5 -foot rubber spacing to 45,000 psi at a 15 -foot rubber spacing.

Drill pipe rubbers as stress reducers have severe drawbacks for the control of bending stresses. The rubbers do not stay in position reliably. Slow drilling rates and heave compensation contribute to excessive wear and rubber displacement. With the heave compensator in use, the relative vertical motion betweeen the compensated drill string and the vessel is greatly increased leading to accelerated rubber wear and displacement when passing through the guide shoe. An alternate solution is the use of
special heavy wall pipe with integral machined hubs replacing the "moveable" rubbers. The increased wall thickness of the heavy wall pipe would also provide for longer fatigue life. The design, test, and operational use of heavy wall drilling joints is described below.

\section*{TUBE DESIGN}

The desired design was a heavy wall pipe with a hub spacing (stabilizers) to minimize bending stresses due to deflection of the tool joints while the pipe is in the guide shoe. The heavy wall pipe was to be used only at the upper section of the drill string exposed to the bending stresses in the guide shoe. The optimum design was to yield the maximum cycles to failure for the following design and handling limitations as excerpted from the request for proposal:
1) Maximum outside diameter of tool joints and hubs: 7 inches.
2) Minimum internal diameter: 4-1/8 inches (4 inch drift required for wireline coring operations).
3) Tensile load: static maximum 532,000 lbs. Average 400,000 lbs while drilling. Maximum static with 100,000 lbs overpull is 632,000 lbs.
4) Length: 30 feet minimum, 45 feet maximum.
5) Maximum weight: 2,500 lbs per joint for ease of handling.
6) Design for collar type elevators (slip type will not be used) compatible with normal rig tools.
7) Approximate maximum 400 feet of heavy wall pipe would be in drill string at any one time.
8) Design stiffness should allow for gradual radius of curvature with no stress riser at connection to 5-inch, \(19.5 \mathrm{lbs} / \mathrm{ft}, \mathrm{S}-135\). Present pipe has \(5-1 / 2\) inch API F.H. tool joints.

Resulting design specifications will include, but not be limited to, following specifications:
1) Wall thickness.
2) Type and size of connections.
3) Recommended mechanical properties (ultimate strength, yield, etc.).
4) Hub dimensions and spacing.
5). If other than 5-1/2 inch API F.H. connection specified, please provide dimension and design of crossover subs required at upper and lower terminations of heavy wall (nominal 300-400 ft assembly).
6) Calculations and assumptions used to arrive at optimum design.

Dr. Arthur Lubinski responded to the request for proposal meeting the above requirements. The development of the design is found in Reference 1 which is included in Appendix I. His essential findings and recommendations were:
1. An O.D. of 5.725 inches (wall thickness of 0.8 inches) was selected.
2. Hub spacing to be 5 ft . A 6 or 8 foot spacing could be adopted with a shorter fatigue life.
3. If 500 ft of heavy wall pipe is used with equal bending exposure the fatigue life is 21 years (calendar operational years, not rotating hours). Rotation at a single point under continuous bending would fail the pipe in 17 days.
4. Minimum yield: 120,000 psi.
5. Tube:

Length: 30 ft
O.D.: 5.725 in
I.D.: \(\quad 4.125\) in (4-inch drift)
6. Pipe to have 7-inch O.D. hubs.
7. Provide for elevator suspension (dual elevator handling system to be employed).
8. Notch toughness and fatigue characteristics in seawater to be the same as those of \(\mathrm{S}-135\) steel.
9.

Tool Joints:
\[
\begin{array}{ll}
\text { O.D.: } & 8 \text { in } \\
\text { I.D.: } & 4.125 \text { in (4-inch drift) }
\end{array}
\]

Design to withstand:
(1) \(25,300 \mathrm{ft}-\mathrm{lb}\) static bending moment applied simultaneously with a static pull of \(632,000 \mathrm{lb}\).
(2) In fatigue in seawater, a fully reversed bending moment of \(25,300 \mathrm{ft}-1 \mathrm{~b}\) applied simultaneously with a pull of 400,000 lb.
(NOTE: The final design used a 1/2-inch wall thickness, 5-1/2 inch O.D., and a 4-1/8-inch bore with a 4-inch drift. Hub and tool joint diameters were 7-3/4 inches. The changes were made following the selection of a 5-1/2 inch I.F. connection).

\section*{CONNECTION DESIGN}

After design of the heavy wall pipe tube Dr. P.D. Weiner of Texas A \& M University was selected to propose a design and a test program for a new tool joint (connection). An analysis was made to determine the optimum heavy wall design. The following connections were investigated (Ref. 2):
\begin{tabular}{ll}
\(6-5 / 8\) inch & Full Hole \\
\(5-1 / 2\) inch & I.F. \\
\(5-1 / 2\) inch & Regular \\
\(5-1 / 2\) inch & Full \\
NC 56 & \\
\(6-5 / 8\) inch & Regular \\
\(6-5 / 8\) inch & H-90 \\
NC 61 & \\
7 inch & H-90 \\
\(5-1 / 2\) inch & H-90
\end{tabular}

The optimum connection proved to be a 5-1/2-inch Internal Flush (I.F.) with an O.D. of \(7-3 / 4\) inches and an I.D. of \(4-1 / 8\) inches. Make-up torque was calculated at \(53,247 \mathrm{ft}-1 \mathrm{~b}\) and the force to open the connection at \(2,287,568 \mathrm{lbs}\). (NOTE: Industry recommendation, as per Reed Tool Company, is 44,000 lbs for make-up torque.)

Other considerations in the design are bending strength ratios and moment of inertia ratios. The bending strength ratio of a connection is the ratio of the box section modulus to the pin section modulus. The American Petroleum Institute (API) states that a bending strength ratio of 2.50:1 is generally accepted as an average balanced connection with an acceptable range of \(3.20: 1\) to \(1.90: 1\) depending on drilling conditions (Ref. 3). The API recommendations are for compression members where the stress arises from make-up torque and bending. The designed connection with a bending strength ratio of 2.06 is reasonable as the connection is used in tension at the top of the string and the box is not subject to wear in the hole.

The ratio of moment of inertia of the tube section to the connection (or hub) should also be optimized. Weiner (Ref. 4) found,
from extensive testing of drill collar connections, that the maximum life of the connection is obtained when the ratio of the moment of inertia of the \(5-1 / 2\) inch tube body (relief) to the connection is from . 28 to .32 . The ratio is . 19 for the design connection. The lower value is considered reasonable as the life of the connection will be extended, and the 10.4 square inches of tube body area is adequate for the tensile loads expected. The minimum yield load of the tube is \(1,248,000\) pounds. The fabrication drawing and specifications for the heavy wall drilling joints are included in Appendix II.

\section*{TEST PROGRAM}

A static test program was undertaken by a contractor to verify the theoretical analysis (Ref. 5). Pertinent parts of Reference 5 are included as Appendix III. The general testing sequence, as excerpted from Appendix III, was as follows:
a) Torque connections to \(60 \%\) of optimum torque.
b) Apply axial load of 400,000 lbs. Remove axial load.
c) Apply bending moment to equal an equivalent deflection of 16 degrees per 100 ft . Remove bending load.
d) Combined load. Apply axial load of 400,000 lb., followed by a bending moment such that the deflection at the connection is the same as that noted under part \(C\). Remove bending load.
e) Break-out connections.

This sequence was repeated for torquing the connections to \(80 \%\), \(100 \%\) and \(120 \%\) of optimum torque with one exception-- Step E was not executed at the completion of \(120 \%\) of optimum torque sequence.

The principal findings of the test program were:
a) At no point during the loading did the shoulders separate. The maximum loading was \(402,025 \mathrm{lb}\) axial combined with a bending moment to bend the test specimen to 16 degrees/100 ft arc.
b) The maximum stress concentration factor for the loading conditions of (a) above is 1.45. This geometric stress concentration is adjacent to a change of section where the tube meets the larger diameter connection.
c) The calculated pin stress at the stress relief groove for a make-up toque of \(53,247 \mathrm{ft}-1 \mathrm{bs}\) ( \(120 \%\) of optimum) with \(400,000 \mathrm{lbs}\) tension and a curvature of 16
degrees/100 ft is 105,626 psi. The contractor's calculated stress from strain gages is on the order of \(165,000 \mathrm{psi}\). The difference may be due to a localized geometrical stress concentration in the stress relief groove. No deformation was apparent and the connection did not open up under the load.

The high stress is due mainly to make up torque and the contractor has proposed to lower the torque to 27,000 ft-lbs to bring pin stresses to 68,000 psi. A make-up torque of \(44,000 \mathrm{ft}-\mathrm{lbs}\) is in accord with field practice and should be used to minimize connection problems.

The pin stresses obtained by the contractor are consistent with similar work done in industry (Ref. 6). The measured stresses on the pin stress relief groove outer surface are higher than those measured on the I.D. of the pin sress relief groove (bore) by a factor of three. Recommended connection make up torque is based on a nominal \(60,000 \mathrm{psi}\) stress across the pin stress relief groove, i.e., average stress through the pin.

DSDP has followed the industry recommendation of \(44,000 \mathrm{ft}-\mathrm{lbs}\) make-up torque and has received adequate service from their heavy wall joints. Reference 5 states that a make-up torque of 27,000 ft-lbs should be used so as not to exceed the stress limitations, but cautions that since only one connection was tested, it might be advisable to test more connections. Additional analysis and testing would need to be considered to verify stress distribution through the pin area and verify that the pin stress readings were valid. However, operational use has substantiated the safety of the higher make-up torque. An analysis which compares the theoretical strains and deflections of the heavy wall joints with the measured values discussed above has been included as Appendix IV. It can be seen from Table I of this comparison that the calculated and measured strain values generally differ by less than ten percent.

\section*{OPERATIONAL USE}

The operational use of the heavy wall drilling joints is determined by the length of drill string deployed and the rate of penetration while drilling. The reason for using the heavy wall joints is to reduce stress at the top of the drill string and thereby increase the fatigue life. Figure 3 shows the conditions of string length and penetration rate under which the heavy wall joints should be used. The heavy wall joints are also used under certain special conditions such as during logging where the drill string is stationary in the guide shoe without rotating and during storms which produce high pitch or roll.

It is usually in borderline situations where the heavy wall joints are used--situations that are imposing high bending stresses repeatedly on the same section of drill pipe. If a storm is producing the situation, then the moving of the heavy wall joints from the casing rack to the rig floor must be done with utmost care. The joints may be stored in a casing rack or in shucks, but they must be available quickly when needed. The heavy wall joints, when used, should extend to at least below the keel of the ship, and be positioned so that a connection is not located at the keel except for passing the keel on the downward or upward movement of the drill string. It has been customary in the DSDP to use ten heavy wall joints at a time. If greater drill string length is required, the heavy wall joints are pulled up, taken out, and replaced with standard drill pipe. The replaced section is then lowered quickly through the guide shoe until the bottom of the hole is reached; then, if still necessary, the heavy wall joints are again inserted in order to drill ahead. For ease of core tally the heavy wall joints should be the same length as the standard drill pipe being used. A lubricant with high ( \(40 \%-60 \%\) ) metallic content, either zinc or lead, should be used when making up a connection with the heavy wall joints. The lubricant should be applied liberally to both the box and the pin threads and to the shoulders. Best-0-Life 270 is an adequate lubricant for this purpose.

Since the heavy wall joints are, by the nature of their function, highly stressed it is important that they be maintained properly and inspected periodically. A magnaflux inspection will reveal tiny fatigue cracks. A log should be kept in which is listed the hours of usage, both rotating and non-rotating. This log can be used as a guide to determine, in conjunction with the inspections, when a heavy wall joint should be removed from service. Not only must the drilling joints themselves be monitored for fatigue or cracks, but the guide shoe through which the drill string passes must also be checked periodically. Repeated use of the heavy wall joints can lead to excessive wear of the guide shoe especially at the top 2 or 3 feet. When this occurs, the worn section must be repaired. With this in mind, it might be advisable in future designs of guide shoes to make the top 5 feet thicker, or replaceable, or with rollers.

It may be noticed from the drawing of the heavy wall drilling joint in Appendix II that both of the end hubs are 18.8 inches long whereas the middle hubs are approximately 13 inchies long. Experience of the DSDP has shown that cracks usually appear first in the threaded portion at either end. The longer (than necessary) length of the end hubs allows for a recut, i.e., cutting off the existing threaded portion and machining new threads. This process has been used successfully to extend the usable life of the drilling joints.

\section*{REFERENCES}
1. Lubinski, Arthur, "Special Heavy Wall Drill Pipe for The Deep Sea Drilling Project", August 1975.
2. Memorandum to the Deep Sea Drilling Project, Mr. Adams from Weatherford/Lamb, Inc., Dr. P.D. Weiner, December 1, 1976.
3. API Recommended Practice for Drill Stem Design and Operating Limits (API RP-7G) Dallas, January 1981 and Supplement 2, 1983.
4. Memorandum Report to the Deep Sea Drilling Project from Dr. P. D. Weiner, dated May 10, 1976.
5. Eichberger, L. C., "Experimental Evaluation of Optimum 5-1/2" I.F. Connection Design". Report submitted by Weatherford/Lamb to the Deep Sea Drilling Project, Scripps Institution of Oceanography, March 1978.
6. Internal Deep Sea Drilling Project memorandum from Mr . B. W. Adams, dated May 8, 1978.


DRILL STRING IN GUIDE SHOE
FIGURE 1


RATE OF PENETRATION (M/HR)


HEAVY WALL DRILLING JOINT GUIDE
FIG. 3

\section*{APPENDIX I}

\section*{SPECIAL HEAVY WALL DRILL PIPE} FOR THE DEEP SEA DRILLING PROJECT

\title{
Deep Sea Drilling Project
}

University of California
Scripps Institution of Oceanography
La Jolla, California 92037
\(\begin{array}{ll}\text { Subject: Transmittal of Results and Report } \\ & \text { Independent Consultant Agreement No. } 0332 .\end{array}\)

Attached is my report entitled "Special Heavy Wall Drill Pipe for the Deep Sea Drilling Project'. The report is presented in two sections, namely the "SPECIFICATION" and the "DEVELOPMENT". As agreed I might, if needed, make a trip to La Jolla.

The essential findings and comments are as follows:
1. You might wish to change and/or complete the specification.
2. I have chosen an OD of 5.725 inches (wall thickness of 0.8 inches). If necessary, an OD of 5.525 inches (wall thickness of 0.7 inches) would also be satisfactory.
3. I have chosen a hub spacing of 5 feet. A spacing of 6 or even 8 feet could be adopted, with a somewhat shorter fatigue life.
4. At the bottom of the guide shoe drill pipe is always bent, except in completely calm seas. If a length (joint) of pipe were rotated and maintained under tension at the bottom of the guide shoe, a fatigue failure could be expected in this length in 17 days. If, on the other hand all of the 500 feet of heavy wall drill pipe is
subjected to equal bending exposure, then no failure should be encountered until 11 years. In normal drilling operations, in which 500 feet of heavy drill pipe are used, all lengths (joints) of pipe are subjected to essentially equal bending exposure. Lengthy rotation of the pipe without simultaneous vertical advance should be avoided.
5. The reason for using heavy wall drill pipe is to improve the fatigue resistance. However with the heavy wall drill pipe, torsional and tensile stresses become smaller, which justifies the value of minimum yield strength of 120,000 psi included in the Specification. It is rather fortunate that a yield strength smaller than 135,000 psi could be tolerated, as in the manufacturing process, thick walls would have to be heated to a higher temperature than ordinary S-135 pipe. With the same chemical composition one could not maintain the same yield value ( \(135,000 \mathrm{psi}\) ). Thus to maintain the same yield value it would be necessary to increase the alloy content of steel, which in turn could make it more brittle and destroy the fatigue characteristic which we must try to maintain.

You could request tool joint design from Drilco in Houston. Please contact there S. T. (Sam) Crews, Manager of Product Engineering.
under separate cover.
As requested I am returning Lith Lockean's report and the Technical Report No. 4.

Yours very truly,


Arthur Lubinski
Technical Consultant

AL:imj
Attachments

\title{
SPECIAL HEAVY WALL DRILL PIPE FOR THE DEEP SEA DRILLING PROJECT
}

Report prepared by
Arthur Lubinski, Technical Consultant

August 6, 1975

\section*{SPECIFICATION}

\section*{SPECIAL HEAVY WALL DRILL PIPE}

Joints (lengths) of special heavy wall drill pipe shall be 30 feet long. ID \(=4.125\) inches (4-inch drift)
\(O D=5.725\) inches
The pipe shall be provided with 7" OD hubs. The pipe and hubs shall be one piece made from a steel bar or a tube. The OD of a hub shall be 7 inches, over a length of 12 inches. The shape of machined surfaces shall be such that stress raisers are avoided. The distances (axis to axis) between hubs (or between a hub and a tool joint) shall be 5 feet.

The provision for elevator suspension shall be the same as in the drill pipe presently used in the Deep Sea Drilling Project.

The minimum yield strength shall not be less than 120,000 psi. The notch toughness, and fatigue characteristics in salt water shall be the same as those of S-135 steel. To ascertain this, bars (or tubes) from one heat will be set aside to make the product. One bar (or tube) will be heat treated. Thereafter specimens will be taken and fatigue tests conducted in conditions similar to tests made on S-135 steel for the Mohole Project.

TOOL JOINTS
\(O D=7\) inches
ID \(=4.125\) inches (4-inch drift)
The tool joints shall be able to withstand the following:
(1) a static bending moment of \(25,300 \mathrm{ft} \mathrm{lb}\) applied simultaneously with a static pull of \(632,000 \mathrm{lb}\).
(2) in fatigue in salt water, a fully reversed bending moment of \(25,300 \mathrm{ft} \mathrm{lb}\) applied simultaneously with a pull of \(400,000 \mathrm{lb}\).

Tool joints may either be (1) machined at the end of special heavy wall drill pipe lengths; or (2) welded to drill pipe lengths.

Tool joints presently used by the Deep Sea Drilling Project are satisfactory and, therefore, similar design and metallurgical properties are desirable.
\(C_{0}=\) pipe curvature at the tool joint
\(\mathrm{C}=\) guide shoe curvature \(=\frac{1}{350 \times 12}=238.095 \times 10^{-6}\) in \(^{-1}\)
Assume first that \(C_{O}=C\), i.e. that drill pipe centralization, thanks to hubs and tool joints, is perfect. This assumption will be removed later.
\[
\sigma_{B}=\text { bending stress }
\]

From Eq. (7), Ref. 1
\[
\sigma_{\mathrm{B}}=\frac{\mathrm{EDC}_{\mathrm{o}}}{2}
\]
\(\mathrm{E}=\) Young's modulus \(=30 \times 10^{6} \mathrm{lb} / \mathrm{in}^{2}\)
\[
\sigma_{\mathrm{B}}=\frac{30 \times 10^{6} \times 238.095 \times 10^{-6} \times \mathrm{D}}{2}=3571.429 \mathrm{D}
\]
\(\mathrm{A}=\) cross -sectional area of pipe wall
Tension \(=400,000 \mathrm{lb}\)
\[
\sigma_{\mathrm{t}}=\text { tensile stress }
\]

Pipe ID \(=4.125\)
\[
\sigma_{t}=\frac{400,000}{\frac{\pi}{4}\left(D^{2}-4.125^{2}\right)}=\frac{509,296}{D^{2}-17.016}
\]

To make allowance for the effect of the tensile stress \(\sigma_{t}\) on fatigue, \(\sigma_{\mathrm{B}}\) must be multiplied by the correction factor \(\boldsymbol{\mathcal { T }}\) (Ref. 2, Eq. (1))
\[
\tau=\frac{\mathrm{t}}{\mathrm{t}-\sigma_{\mathrm{t}}}=\frac{1}{1-\frac{\sigma_{\mathrm{t}}}{\mathrm{t}}}
\]
\[
\sigma_{\mathrm{t}}=\text { tensile stress }
\]
\(\mathrm{t}=\) tensile strength \(=150,000 \mathrm{psi}\)

Thus the bending stress to be considered, i.e. the bending stress adjusted for tension is
\[
\tau \sigma_{\mathrm{B}}=\frac{\sigma_{\mathrm{B}}}{1-\frac{\sigma_{\mathrm{t}}}{\mathrm{t}}}
\]
which is the same as Eq. (2.42) page 99, Ref. 3, with changed notation, except that the latter contains a correction factor k ( K in Ref. 3) to account for the corrosive nature of sea water. \(k=0.9\).
\[
\begin{align*}
\tau \sigma_{\mathrm{B}} & =\frac{\sigma_{\mathrm{B}}}{\mathrm{k}\left(1-\frac{\sigma_{\mathrm{t}}}{\mathrm{t}}\right)} \\
\tau \sigma_{\mathrm{B}} & =\frac{3571.429 \mathrm{D}}{0.9\left(1-\frac{509,296}{\mathrm{D}^{2}-17.106} \times \frac{1}{150,000}\right.} \\
& =\frac{3968.254 \mathrm{D}}{1-\frac{3.395305}{\mathrm{D}^{2}-17.016}} \tag{1}
\end{align*}
\]

Introduction of the coefficient \(k\) is not logical, as the fatigue data to be used are for sea water environment. However, as use of \(k\) yields more conservative results, \(k\) is used in the calculations of this report.

A curve drawn through points for fatigue experiments in sea water is given in Fig. 11, Ref. 4, and Fig. 1, Ref. 5. Stresses which will be considered farther in this report are of the order of \(30,000 \mathrm{psi}\). For such stresses the solid curve is more conservative than the fitted dashed curve B of Fig. 1, Ref. 5. For this reason the solid curve will be used. This curve
is redrawn in the Fig. l of this report.
In Fig. 1, the abscissa is the number of revolutions of drill pipe to failure. The ordinate is the bending stress \(\mathcal{T} \sigma_{B}\) adjusted for tension.

The following table was obtained using Eq. (1).
\begin{tabular}{|c|c|c|}
\hline Wall pipe thickness in & Outside diameter D in & \(\tau \sigma_{B}\) \\
\hline 0.3 & 4. 725 & 52,006 \\
\hline 0.4 & 4.925 & 36,805 \\
\hline 0.5 & 5. 125 & 32,132 \\
\hline 0.6 & 5.325 & 30,162 \\
\hline 0.7 & 5.525 & 29,285 \\
\hline 0.8 & 5.725 & 28,957 \\
\hline 0.9 & 5.925 & 28,945 \\
\hline 1.0 & 6.125 & 29,130 \\
\hline 1.5 & 7.125 & 31,436 \\
\hline 2.0 & 8. 125 & 34,643 \\
\hline 3.0 & 10.125 & 41,840 \\
\hline
\end{tabular}

These results are plotted in Fig. 2.
The bending stress corrected for tension, \(\mathcal{T} \sigma_{B}\), is minimum for wall thickness of 0.9 , which corresponds to \(D=5.925 . \tau \sigma_{B}\) is nearly the same for wall thickness of \(0.8, D=5.725\), which are the values adopted here. It is believed that adequate tool joint design is feasible for an OD not exceeding the permissible value of 7 inches. However, if necessary, a pipe thickness of 0.7 inches would be acceptable too, although this would result in somewhat shorter fatigue life than calculated in this report.

For pipe of wall thickness of 0.8 , various values of the spacing between hubs (and between a hub and a tool joint) will now be considered. It is assumed that the OD of hubs is the same as that of tool joints.

From Eq. (12), Ref. 1, we obtain the pipe curvature \(C_{0}\) (which is proportional to the bending stress) as function of the guide shoe curvature \(C\).
\[
C_{0}=C \frac{K L}{\operatorname{Tanh} \overline{K L}}
\]
\(\mathrm{L}=\) half distance between hubs (and between a hub and a tool joint) K is given by Eq. (2t) Ref. 1.

\(\mathrm{T}=\) tension in the pipe \(=400,000 \mathrm{lb}\)
\(\mathrm{E}=\) Young's modulus
\(I=\) moment of inertia with respect to diameter
\[
\begin{aligned}
I & =\frac{\pi}{64}\left(D^{4}-4.125^{4}\right)=\frac{\pi}{64}\left(5.725^{4}-4.125^{4}\right) \\
K & =\sqrt{\frac{0.4 \times 10^{6}}{30 \times 10^{6} \times \frac{\pi}{64}\left(5.725^{4}-4.125^{4}\right)}}=0.018605 \mathrm{in}^{-1}
\end{aligned}
\]

The above equation may also be written as follows:
\[
\left(\mathcal{T} \sigma_{B}\right)_{0}=\tau \sigma_{B} \frac{K L}{\text { TanhKL }}
\]
in which \(\boldsymbol{\tau} \sigma_{\mathrm{B}}\) corresponds to perfect centralization \(\left(\boldsymbol{\mathcal { T }} \boldsymbol{\sigma}_{\mathrm{B}}=28,957 \mathrm{psi}\right)\), and \(\left(\mathcal{T} \sigma_{\mathrm{B}}\right)_{\mathrm{o}}\) corresponds to actual centralization.


The last column in the above table is obtained from Fig. 1. The shorter the spacing between hubs (and a hub and a tool joint), the greater is the number of revolutions to failure, i. e. the longer is the life of the pipe. A spacing of 5 feet is adopted in this project. The above table indicates how much could be gained through a shorter spacing, or lost through a longer spacing.

From now on the subscript "o" will not be used in \(\left(\boldsymbol{\tau} \boldsymbol{\sigma}_{\mathrm{B}}\right)_{\mathrm{o}}\) when referring to the adopted value, \(\mathcal{T} \sigma_{\mathrm{B}}=31,900 \mathrm{psi}\).

The corresponding value of revolutions to failure \(N=730,000\) would hold true for a length of pipe (commonly called joint of pipe) which would be permanently located at the bottom of the guide shoe. Such a length of pipe would be permanently bent, while a length located half way into the guide shoe would be subjected to bending only when the vessel angular deflection from vertical is between \(4^{\circ}\) and \(8^{\circ}\); finally a length of pipe located at the top of the guide shoe would be bent only when vessel deflection is \(8^{\circ}\).

Heavy drill pipe should be used in such a way that every length is subjected to equal bending exposure. In other words lengths of heavy pipe should not always be run in the same sequence.

The resultant angular motion of the pitch and roll of the vessel will be referred to as pitch.

During a pitching motion of amplitude \(\boldsymbol{\alpha}\), the pipe is rotated while drilling or coring. Therefore the angular deflection of the ship varies during one
quarter of the pitch cycle between \(\boldsymbol{\alpha}\) and zero. As a result, the number of revolutions to failure doubles if the pipe is run so as to achieve equal exposure to bending, with respect to the case of the same joint of pipe being located at the bottom of the guide shoe. Thus \(\boldsymbol{\tau} \sigma_{\mathrm{B}}\) becomes
\[
\tau \sigma_{\mathrm{B}}=2 \times 730,000=1,460,000=1.46 \times 10^{6} \text { revolutions to failure. }
\]

An estimate of Glomar Challenger pitch history (actually the combination of pitch and roll) is as follows
\begin{tabular}{ccc} 
Pitch Interval & & \begin{tabular}{l} 
Fraction of Time \\
\(7^{\circ}-8^{\circ}\)
\end{tabular} \\
\(6^{\circ}-7^{\circ}\) & 0.001 \\
\(5^{\circ}-6^{\circ}\) & 0.001 \\
\(4^{\circ}-5^{\circ}\) & & 0.008 \\
\(3^{\circ}-4^{\circ}\) & & 0.02 \\
\(2^{\circ}-3^{\circ}\) & & 0.05 \\
\(0-2^{\circ}\) & & 0.12 \\
& & \(\underline{0.80}\) \\
& & \\
& & 1.000
\end{tabular}

The number of revolutions to failure, taking this pitch distribution into consideration, is calculated in the following table.


Average number of revolutions
\[
\text { to failure }=\frac{1}{0.011939 \times 10^{-6}}=83.759 \times 10^{6}
\]

The above table is explained in the text which follows.

Assume that 500 feet of heavy drill pipe are being used in proper sequence to achieve equal exposure to bending. As the height of the guide shoe is \(350 \mathrm{ft} x \sin 8^{\circ}=49 \mathrm{ft}\), the previously calculated number of revolutions to failure ( \(1.46 \times 10^{6}\) ) must be multiplied by \(500 / 49\). For an \(8^{\circ}\) pitch all the pipe in the guide shoe is bent. Consider for instance \(3.5^{\circ}\) average pitch. Then only the fraction (3.5)/8 of the pipe in the guide shoe is bent. Thus the number of revolutions to failure becomes
\[
1.46 \times 10^{6} \times \frac{500}{49} \times \frac{8}{3.5}
\]

This number pertains to a case of constant pitch of 3.5 degrees. In other words this would have been the number of revolutions to failure if the pitch did not vary with time but remained equal to \(3.5^{\circ}\) until failure.

In such a case the fraction of life expended per cycle would have been the reciprocal of the number of revolutions to failure. As actually the 3.5 degrees average pitch occurs only a fraction 0.05 of time, this reciprocal must be multiplied by 0.05 . Thus the fraction of life expended for \(3.5^{\circ}\) average pitch becomes
\[
\frac{1}{1.46} \times 10^{-6} \times \frac{49}{500} \times \frac{3.5}{8} \times 0.05
\]
which is entered in the table.

Fractions of life expended are additive, and their sum is entered in the above table.

The reciprocal of their sum is the average number of revolutions to
failure.

Let us assume that the drilling string is rotated by 60 RPM. Then
\[
84 \times 10^{6} \mathrm{Rev}=84 \times 10^{6} \mathrm{sec}=\frac{84 \times 10^{6}}{3600 \times 24} \text { days }=969 \text { days }
\]

As drilling or coring is conducted only \(1 / 4\) of total time, the above number becomes
\[
969 \times 4=3876 \text { days }=10.6 \text { years }
\]

It should be emphasized once again that this value is predicated upon the assumption that the heavy wall drill pipe is used in such a manner that all lengths (joints) of pipe are subjected to equal bending exposure. A pipe rotated while permanently located at the bottom of the guide shoe, will fail after \(1.46 \times 10^{6}\) revolutions or about \(1.46 \times 10^{6} \mathrm{sec}=17\) days.

In the Specification a minimum yield strength of 120,000 psi has been written. Justification of this value is given below

Tensile stress \(\sigma_{\mathrm{t}}=\frac{632,000 \mathrm{lb}}{\mathrm{A}}=\frac{630,000}{\pi}=51,059 \mathrm{psi}\) \(\frac{\pi}{4}\left(5.725^{2}-4.125^{2}\right)\)

Bending stress \(=\sigma_{B}=\frac{\mathrm{EDC}}{2} \times \frac{\mathrm{KL}}{\operatorname{TanhKL}}=3,571 \mathrm{D} \times \frac{\mathrm{KL}}{\text { Tanhkl }}\)
\(=3,571 \times 5.725 \times \frac{\mathrm{KL}}{\operatorname{TanhKL}}=22,526 \mathrm{psi}\)
\(\sigma_{t}+\sigma_{B}=73,585\)
Using a coefficient of safety of 1.6
\[
\sigma_{\mathrm{t}}+\sigma_{\mathrm{B}}=1.6 \times 73,585=117,736 \mathrm{psi}
\]
which shows that a minimum yield strength of \(120,000 \mathrm{psi}\) is adequate as far as tension and bending are concerned.

From present Deep Sea Drilling Project operations we know that \(5^{\prime \prime} 19.5 \mathrm{lb} / \mathrm{ft}\) drill pipe is adequate in torsion. In heavy wall drill pipe the torsional stress will be smaller in the ratio of wall cross-sectional areas, and larger in the ratio of O.D. 's.
\[
\frac{5.275}{12.378} \times \frac{5.725}{5}=0.488
\]

The ratio of yield strength \(s\) is
\[
\frac{120,000}{135,000}=0.889
\]

Thus a minimum yield strength of \(120,000 \mathrm{psi}\) is also adequate as far as torsion is concerned.

It is written in the Specification that tool joints must be able to withstand a bending moment of \(25,300 \mathrm{ft} \mathrm{lb}\). The calculation from which this value has been obtained is as follows.
\(M_{B}=\) EIC \(_{o}\)
\(=30 \times 10^{6} \frac{\mathrm{lb}}{\mathrm{in}^{2}} \times \frac{\pi}{64}\left(5.725^{4}-4.125^{4}\right) \mathrm{in}^{4} \times \frac{1}{350 \times 12} \times 1.1017 \mathrm{in}^{-1}\)
\(=303,120\) in \(\times \mathrm{lb}=25,260 \mathrm{ft} \times \mathrm{lb}\)

\section*{REFERENCES}
1. "Maximum Permissible Dog-Legs in Rotary Boreholes" by Arthur Lubinski. Transactions of AIME 1961, Vol. 222.
2. "The Effects of Drilling Vessel Pitch or Roll on Kelly and Drill Pipe Fatigue" by John E. Hansford and Arthur Lubinski.

Transactions of AIME 1964, Vol. 231.
3. "Deep Sea Drilling Project, Technical Report No. 4", Scripps Institution of Oceanography, University of California at San Diego.
4. "Drill-Pipe Fatigue Failure" by H. M. Rollins, The Oil and Gas Journal, April 18, 1966.
5. "Drill String Analysis Report for Deep Sea Drilling Project", by James C. Lockman, Global Marine Inc., February 4, 1975.



Some Comments on the Report,
"Special Heavy Wall Drill Pipe for the Deep Sea Drilling Project"
By
Arthur Lubinski
1) Lubinski says the introduction of the coefficient \(K\) is not logical (Development, p. 2). The fatigue data from the Rollins paper, Fig. 11, is for full-sized \(\mathrm{S}-135\) drill pipe testing in sea water. At 60 cycles/ min and \(10^{6}\) cycles to failure, the test duration was 277 h 47 min . Actual drill pipe is subjected to sea water corrosion for much longer periods, so use of the coefficient to account for corrosion over a longer period than that in the fatigue tests is logical. Perhaps a \(K=0.9\) is too low, but \(K=1.0\) must be too high.
2). In paragraph 3, Development, p. 5, Lubinski states that "a length of pipe permanently located at the bottom of the guide shoe would be permanently bent...", and "a length of pipe located at the top of the guide shoe would be bent only when vessel deflection is \(8^{\circ \prime \prime}\). Since the roll and pitch is oscillatory about a mean value of zero, no point in the pipe is permanently bent. Roll and pitch less than \(8^{\circ}\) does not cause the pipe at the bottom of the guide shoe to bend, while pipe at the top of the guide shoe bends when the roll and pitch is greater than zero.
3) Lubinski uses a factor of 2 (in revolutions to failure) to account for the cyclic nature of the pitch (or roll). This is an upperbound estimate (see Lubinski's Ref. 3, p. 105), and the lowerbound is 1.47 . The factor used in Ref. 3, 1.57, is my earlier estimate for this factor, and is what I propose to use in my analysis.
4) The fatigue curve used by Lubinski is the curve drawn in the Rollins paper (Lubinski Ref. 4). Seven of 15 test points lie below this curve, so it is not a conservative curve. The fatigue curve \(I\) used with \(\sigma=1102.3\), \(m=3.82\) and \(K=0.9\) is more conservative above \(23 \mathrm{KSI}\left(<2 \times 10^{6}\right.\) cycles and less conservative below \(23 \mathrm{KS}\left(>2 \times 10^{6}\right.\) cycles). If your operating experience could give us a better estimate of the fatigue curve, we can easily fit it into the program.


\section*{APPENDIX II}

\section*{FABRICATION DRAWING AND SPECIFICATION FOR \\ HEAVY WALL DRILLING JOINT}


\title{
DEEP SEA DRILLING PROJECT \\ SPECIFICATION: 0G-0610-06 \\ PROCUREMENT OF HEAVY WALL DRILL JOINTS \\ February 6, 1984
}

\section*{General Description and Intended use}

The Deep Sea Drilling Project, which operates the drillship GLOMAR CHALLENGER intends to procure special design, heavy wall drill joints to run at the top end of the drill string. This design will minimize tensile and cyclical stresses in the drill pipe rotary connections that are subjected to high tensile and bending loads in the CHALLENGER'S guide shoe or horn. Drill pipe in the guide shoe is nominally subjected to 400,000 lbs. tensile loading in combination with \(16^{\circ} / 100 \mathrm{ft}\). bending.

\section*{Design}

The heavy wall drill joints shall be machined as per Deep Sea Drilling Project Drawing No. D-0523-05. Practice and workmanship shall be in accord with API Specification 7.

\section*{Rotary Connections}

\section*{Connections}

5-1/2" Internal F1ush

\section*{Shoulders}

They are to be 7.75 inches O.D. and a minimum of 13 inches long. Surface finish is 125 (face 75). If machining to \(7.750 . D\). does not clean up the shoulder completely, the hot rolled, mill finish is acceptable. Surface imperfections are to be removed by grinding but the removal of such imperfections shall not result in stock removal in excess of 0.125 inches.

\section*{Threads}

Threads must be hob cut, or cut by numerical control, and cold worked. They are to be treated witha suitable anti-galling treatment.

\section*{Stress Relief Grooves}

The connections shall have stress relief grooves. The grooves shall be cold worked.
```

Deep Sea Drillıng Project
Specification: GG-0610-06
Procurement of Heavy Wall Drill Joints
February 6, }198
Page 2

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Hubs
Integrally. machined hubs are to be equally spaced between the rotary connections. The hubs are 7.75-inches 0.D. and 13-2nches long. They will be apr coimately five feet on centers depending on the drill collar bar length.

The transicion from the tube to the box connection is via a le,
5.68 -inch O.D. elevator shoulder an 1 an \(18^{\circ}\) Laper. The transit 4 tube to the elevator shoulder is a 1.5 -inch radius tangent th. The transition from the elevator shoulder to the \(18^{\circ}\) tap \(1 . \mathrm{r}^{\circ}\) also +5 -inch radius, tangent to both surfaces.

The \(18^{\circ}\) taper, the 5.68 -inch 0.D. elevator shoulder, the 4 -inches of 5.50 inch O.D. tube adjacent to the hubs and the transition radii are to be cold worked:

\section*{Marking}

A flat will be milled or ground in the first hub above the pin end. The manufacturer's number and connection identification are to be stamped on the flat.

Trepanning
A. Drij.ling Joints

If the bar is to be trepanned from both ends, the manufacturer must ensure the bores meet at midpoint of center hub. Allowable longitudinal tolerance is \(\pm 3.5\) inches from center hub midpoint. Any step resulting from the trepanning should be removed by honing to a radius of at least . 425 inches.

Drift
The joints mast pass a 10 -foot long 4.0 inch drift.

\section*{Material Properties}

\section*{Material}

AISI 4145 or AISI \(43 \times X\). Series
The joints nust exhibit the following mechanical properties at the 5.7-inch round levei (approximately one-inch below the 7.75-inch 0.D.).

Deep Sea Drilling Project
Specification: OG-0610-06
Procurement of Heavy Wall Drill Joints
February 6, 1984
Page 3
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Tensile Strength - min 140 KSI
Yield Strength - min 120 KSI
Elongation - min 14%
Toughness - Either Charpy or Izod impact test may be used.
Tests shall conform to ASTM E23-72
Charpy (Specimen A) - min 60 ft-1bs
Izod (Specimen D) -min 40 ft-lbs

```

At the minimum, the manufacturer will physically test each heat of steel used to demonstrate that the above specifications are met. If one heat is used, two bars will be tested. The manufacturer will supply DSDP with copies of the test results.

\section*{Inspection and Quality Control}

Each joint will be completely inspected for any defects that would initiate a structural, fatigue, or corrosion failure, i.e., every square inch of tube wall is to be inspected. The manufacturer will supply DSDP with copies of the test results.

The hardness of each rotary connection pin is to be neasured. Hardness measurement may be made on blanked pin. The pin hardness measurements are to be identified by the manufacturer's joint number and supplied to DSDP.

\section*{APPENDIX III}

\section*{EXPERIMENTAL EVALUATION OF OPTIMUM}

5-1/2" I.F. CONNECTION DESIGN

\title{
EXPERIMENTAL EVALUATION OF OPTIMUM 5-1/2" I.F. CONNECTION DESIGN
}

\author{
L. C. EICHBERGER \\ Manager, \\ Engineering and Technical Services
}

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}
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March, 1978

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1.0 SUMMARY
2.0 CONCLUSIONS
3.0 RECOMMENDATIONS
4.0 EXPERIMENTAL WORK
4.1 TEST FRAME
4.2 TEST CONFIGURATION
4.3 DATA COLLECTION AND MEASURING SYSTEM
4.4 TEST PROCEDURES
4.4.1 Make-up Torques
4.4.2 Axial Load
4.4.3 Bending Load
4.4.4 Combined Load - Axial and Bending
4.4.5 Break-out Torque
5.0 RESULTS AND DISCUSSION
5.1 GENERAL INFORMATION
5.2 MAKE-UP STRESSES
5.3 STRESSES DUE TO AXIAL LOAD
5.4 STRESSES DUE TO BENDING LOAD
5.5 STRESSES DUE TO COMBINED AXIAL AND BENDING LOAD

\section*{LIST OF TABLES}
Table 1 Calculated Axial Stresses
Table 2 Average Axial Stress At Stress Relief Groove Of Connection Due to Make-up
Table 3 Average Axial Stress At Stress Relief Groove Of Connection Due to Axial Load
Table 4 Axial Stress At Stress Relief Groove Of Connection Due ToAxial, Bending And Combined Axial And Bending - Odd Gages
Table 5 Axial Stress At Stress Relief Groove Of Connection^To Axial, Bending And Combined Axial And Bending - Even Gages
Table 6 Axial Stress At Stress Relief Groove Of Connection Due To Combined Loading

\section*{LIST OF ILLUSTRATIONS}
\begin{tabular}{|c|c|}
\hline Figure No. & Subject \\
\hline 1 & Test Frame And Specimen Configuration \\
\hline 2 & Loading Modes Of Test Configuration \\
\hline 3 & Strain Gage Locations \\
\hline 4 & Average Axial Stress At Stress Relief Groove Of Connection Due To Make-up (120\% Optimum Torque Case) \\
\hline 5 & Average Hoop Stress At Stress Relief Groove Of Connection Due To Make-up (120\% Optimum Torque Case) \\
\hline 6 & Average Axial Stress At Stress Relief Groove Of Connection Due To Axial Load (120\% Optimum Torque Case) \\
\hline 7 & Average Hoop Stress At Stress Relief Groove Of Connection Due To Axial Load (120\% Optimum Torque Case) \\
\hline 8 & Axial Stress At Stress Relief Groove Of Connection Due To Bending Load - Odd Gages (120\% Optimum Torque Case) \\
\hline 9 & Hoop Stress At Stress Relief Groove Of Connection Due To Bending Load - Odd Gages (120\% Optimum Torque Case) \\
\hline 10 & Axial Stress At Stress Relief Groove Of Connection Due To Bending Load - Even Gages (120\% Optimum Torque Case) \\
\hline 11 & Hoop Stress At Stress Relief Groove Of Connection Due To Bending Load - Even Gages (120\% Optimum Torque Case) \\
\hline
\end{tabular}

The data for the torque make-up of the test configuration for the \(120 \%\) optimum torque case is taken to be representative of the conditions which exist in the connection. The make-up stress in the stress relief groove of the connection is 1.76-1.81 greater than the calculated stress for the \(100 \%\) optimum torque case. Tensile axial stresses are present in a region adjacent to the shoulder of the connection in the box, instead of, compressive stresses indicating the presence of local bending.

The average stress values are used to describe the conditions which exist in the connection due to an axial load. The average axial stress at the stress relief groove of the connection is 1.07-1.29 greater than the calculated value for an axial load of \(402,025 \mathrm{lb}\). The maximum axial stress in the test configuration for an axial load occurs at the base of the fillet radius where the tube intersects the hub of the drilling sub. This stress is 1.17-1.40 greater than the stress in the tube.

The stresses in the connection produced by a bending moment are inconsistent, however, they represent the condition in the connector of the drilling sub when it is in contact with the horn on a drilling ship. The point of maximum stress in the test configuration is at the base of the fillet radius where the tube and hub intersect. The axial stress, at this point, is \(1.18-1.19\) greater than the bending stress in the tube at the center of the configuration.

The axial stress in the stress relief groove of the connection for a combined axial load of \(402,025 \mathrm{lb}\). and a bending moment (one which produces a deflection in the test configuration of \(16^{\circ}\) per 100 ft .) is within +1957 psi and -4029 psi of the calculated value of 27,047 psi. The maximum axial stress in the test configuration for the combined loading is at the base of the fillet radius, and is greater than the axial stress in the tube at the center of the test configuration by a factor of 1.33-1.45.

The axial stress in the stress relief groove of the connection produced by a make-up torque of \(47,124 \mathrm{ft}-1 \mathrm{~b}\), an axial load of \(402,025 \mathrm{lb}\). and a bending moment (one which will produce a deflection in the test configuration of \(16^{\circ}\) per 100 ft ) exceeds the yield strength of the material.

\subsection*{2.0 CONCLUSIONS}

The test results of this investigation support the following conclusions:
a) The calculated value for make-up stress in the stress relief groove of the connection, in general, is substantially lower than the stress in the connection.
b) The connection yields, when the make-up torque is equal to, or greater than, \(100 \%\) optimum torque or \(47,124 \mathrm{ft}-1 \mathrm{~b}\), and for an axial load of \(402,025 \mathrm{lb}\). and a bending moment which will produce a deflection of \(16^{\circ}\) per 100 ft . in the test configuration.
c) The maximum stress concentration factor for the test configuration subjected to an axial load of \(402,025 \mathrm{lb}\). and a bending moment which produces a deflection in the test configuration of \(16^{\circ}\) per 100 ft. , is 1.45.

\subsection*{3.0 RECOMMENDATIONS}

Based on the test results of this investigation, the following recommendations are made:
a) Reduce the \(100 \%\) optimum torque from \(47,124 \mathrm{ft}-1 \mathrm{~b}\) to approximately \(27,000 \mathrm{ft}-1 \mathrm{~b}\). The \(27,000 \mathrm{ft}-1 \mathrm{~b}\) of torque will produce an axial stress at the stress relief groove of the connection of 67,723 psi (Table 1), or the calculated value.
b) Since the recommendation in (a) is based on the test results of this investigation, then it is strongly recommended to test another instrumented connection in a torsion machine to validate the test results.

\subsection*{4.0 EXPERIMENTAL WORK}

\subsection*{4.1 TEST FRAME}

The principal function of the test frame is to hold the test configuration in position and to provide a means through which to apply an axial load and a bending moment.

Figure 1 shows the basic details of the test frame. The test frame consists of a horizontal lower frame with integral vertical end members A which supports a removable upper frame B. The lower frame and end members are made from large OD pipe, while the upper frame is a composite of welded I-beams and plate. The test configuration \(C\) is held in a horizontal position by pulling adaptors \(D\) which are attached to a fixed bearing support \(E\) at one end, and by a horizontal support \(F\) at the other end. The horizontal support allows free movement of the test configuration in the direction of the configuration's axial axis of symmetry. The pulling adaptors are fitted with self-aligning ball bushings to provide the test configuration with rotational end constraints.

The axial load is applied to the test configuration through the hydraulic cylinder G. The load, which produces the bending moment, is applied through the chain link straps \(H\), the loading beam I and hydraulic cylinder J.

The make-up and break-out of the test configuration's connections is also done while the test configuration is in the test frame. The makeup and break-out is accomplished by the chain tong and back-up shown in Fig. 2a.

\subsection*{4.2 TEST CONFIGURATION}

The test configuration consist of three drilling subs, as shown in Fig. 1. The drilling subs are machined from \(7-3 / 4^{\prime \prime} 0 D \times 4-1 / 8^{\prime \prime}\) ID, AISI 4145 Q \& T, 285-341 BHN specially selected material according to specifications established by the Deep Sea Drilling Project, Scripps Institution of Oceanography. The drilling sub connection is the \(5-1 / 2^{\prime \prime}\) I.F. connection with a special stress relief groove specified by Dr. P. D. Weiner. The pulling adaptor was provided with a 6" Acme (2 thread/inch) connection.

A total of forty (40) strain gages and sixteen (16) fatigue gages are installed on the drilling subs, as shown in Fig. 3. The strain gages used are a single element foil gage : with a \(1 / 8^{\prime \prime}\) gage length (MicroMeasurements gage EA-06-125BT-120). The majority of the gages are installed in two rows, along the axial axis of symmetry and diametrically opposed. The exception to this, is at the stress relief groove and the shoulder of the \(5-1 / 2^{\prime \prime}\) I.F. connection, where a two gage \(90^{\circ}\) rosette is installed - one axial and one circumferential.

\subsection*{4.3 DATA COLLECTION AND MEASURING SYSTEM}

The strain gages were connected to a forty (40) channel BLH Digital Strain Gage Scanning Unit 1200A. The unit has the capability of automatically scanning each channel, conditioning the signal and displaying the strain value on a LED display and printing the strain value out on a built in printer.

The Scanning Unit is interfaced to a Hewlett Packard Calculator - Computer 9825A with a Digital Plotter - Printer 9871A. Software was developed for the 9825A Computer to allow the Computer to receive and store the strain values from the BLH Strain Gage Scanning Unit on command. Software was also developed to process the data and print it out in controlled format form on the printer, as well as, to plot the data.

Deflections of the test configuration are read from five (5) Mitutoyo Dial Indications of 0.001 " increments over a \(2^{\prime \prime}\) range. The dial indicator locations are shown in Fig. 2b and in Fig. C1 in Appendix C.

The pressure to the hydraulic cylinders for the torque make-up and bending test was read on a 1,500 psi Marsh, Type 100-3 pressure gauge. The smallest division reads 10 psi , which enables an estimate of the pressure reading to 5 psi . The pressure to the hydraulic cylinder for the axial load was read on a 10,000 psi Marsh, Type 100-3 pressure gauge. The smallest division reads 100 psi, which enables an estimate of the
pressure to 50 psi . The pressure gauges were calibrated on a dead weight tester before the start of the testing.

\subsection*{4.4 TEST PROCEDURES}

The general testing sequence is as follows:
a) Torque connections to \(60 \%\) of optimum torque.
b) Apply axial of 400,000 lbs. Remove axial load.
c) Apply bending moment to equal an equivalent deflection of \(16^{\circ}\) per 100 ft . Remove bending load.
d) Combined load. Apply axial load of 400,000 1b., followed by a bending moment such that the deflection at the connection is the same as that note under part C. Remove bending load.
e) Break-out connections.

This sequence was repeated for torquing the connections to \(80 \%, 100 \%\) and \(120 \%\) of optimum torque with one exception, and that is, step E was not executed at the completion of \(120 \%\) of optimum torque sequence.

The detailed test procedure followed under the above steps is as follows:

The test configuration was initially assembled using Weatherford/Lamb Lub-Guard thread compound on the threads and shoulders of the connection. It was then placed in the test frame and readied for the first test sequence.

\subsection*{4.4.1 Make-up Torque}

The make-up torque was applied to the test configuration by a chain tong which had a four (4) foot arm. The test configuration was constrained from rotating by a chain back-up. The chain tong was actuated by a hydraulic cylinder, as shown in Fig. 2a, and made-up both connectionsat one time. The test configuration was first made-up to a hand tight position, the strain gages were zeroed and their values were recorded. The chain tong was then attached to the drilling sub hub for torquing. Before a torque was applied, each connection was marked so that the amount of turns could be measured for a given torque. The torque was applied in consistent increments for all make-up tests. At each torque level, the weight of the chain tong was removed from the test configuration before the strain gages were read. Also the turns for each connection were noted and recorded.

\subsection*{4.4.2 Axial Load}

The test configuration was rotated so that the strain gages on the middle drilling sub were in a vertical plane, odd numbered gages on top and even numbered gages on the bottom. In the no-load state, the strain gages were zeroed and their values were recorded. The axial load was applied in equal and consistent increments for all axial load tests. After each load increment, the strain gages were read.

\subsection*{4.4.3 Bending Load}

In the no-load state, the strain gages were zeroed and their values were recorded. Dial indicators were positioned and set and their initial readings were noted and recorded. The bending load was applied in consistent increments for all bending tests. After each load increment, the strain gages were read and the dial indicator readings were recorded.

\subsection*{4.4.4 Combined Load - Axial and Bending}

In the no-load state, the strain gages were zeroed and their values were recorded. An axial load of \({ }^{-402,025 ~ l b s . ~ w a s ~ a p p l i e d ~ t o ~ t h e ~ t e s t ~}\) configuration and the strain gages were read. The dial indicators were positioned and set and their initial readings were noted and recorded. The bending load was applied using the procedure described under Section 4.4.3.

\subsection*{4.4.5 Break-out Torque}

Break-out torques for each 5-1/2" I.F. connection were noted and recorded. Each connection was backed out until the shoulders of the connection separated by approximately \(1 / 2^{\prime \prime}\). The shoulders were inspected for damage and re-doped if no damage was detected. The test configuration was readied for the next testing sequence.

\subsection*{5.0 RESULTS AND DISCUSSION}
5.1 GENERAL INFORMATION

Table 1 is a summary of calculated values of the axial stress in the connection for make-up torque, axial and bending loads from Appendix D. A torque of \(47,124 \mathrm{ft}-1 \mathrm{~b}\) is the optimum torque value used in this report to establish the \(60 \%, 80 \%, 100 \%\) and \(120 \%\) optimum torque cases (OTC). The torque of \(53,247 \mathrm{ft}-1 \mathrm{~b}\) is the corrected value for the optimum torque and results from a correction to an error found during the preparation of Appendix D.

The strain gages data for the \(60 \%, 80 \%, 100 \%\) and \(120 \%\) OTC and the corresponding axial and hoop stress values can be-found in Appendix A.

Appendix B contains data on connection advancement for each torque increment and for each optimum torque case. It also contains information on strain gage misalignment due to make-up.

Deflection data due to the bending load and the combined loading of axial and bending for the \(60 \%, 80 \%, 100 \%\) and \(120 \%\) OTC can be found in Appendix C.

\subsection*{5.2 MAKE-UP STRESSES}

Table 2 shows the average axial stress at the stress relief groove of the connection for each of the optimum torque cases. The values in Table 2 shows no consistency between connections and optimum torque cases.

The \(120 \%\) OTC is presented as giving the truest stress values in the connection's pin and box due to make-up. The reason for this is that at each torque increment, the constraints on the test configuration were adjusted so that it would rotate freely before the strain gages were read. In previous make-ups, only the weight of the chain tong was removed from the test configuration before the strain gages were read. Since the test configuration was not checked to see if it could be rotated, then there is the possibility that the test configuration was subjected to a bending moment. The bending moment can come about by the hub of the test configuration rolling up the incline plane of the chain back-up and locking in place preventing the hub from returning to its free position when the chain tong was removed after each torque increment. This concept is supported by the test data which shows unusually high axial stress in the tube of the test configuration for all optimum torque cases except the \(120 \%\) OTC, (Table A1c, A5c, A9c and A13c in Appendix A).

Figures 4 and 5, respectively, show the make-up stress in the stress relief groove of the connection for the \(120 \%\) OTC to be practically the same for each connection. The slight change in shape in the initial part of the curve is probably due to overcoming tolerance differences in pin and box of connection which takes place until the shoulders of the connection come into solid contact at approximately \(10,000 \mathrm{ft}-7 \mathrm{~b}\).

Comparison of the axial stress in the stress relief groove in the pin of 119,240-122,854 psi (Table 2) with its calculated value of 67,726 psi for a \(47,124 \mathrm{ft}-1 \mathrm{~b}\) torque and \(120 \%\) OTC (Table 1), shows the axial stress to be \(1.76-1.81\) greater than the calculated.

Comparison of the axial stress in the vicinity of box shoulder (0.260" from the shoulder) of 2959 psi at point 2 and 3214 psi at point 13 for a \(47,124 \mathrm{ft}-1 \mathrm{~b}\) torque (Table A13c, Appendix A) with the calculated box shoulder stress of \(-96,708 \mathrm{psi}\) (Table 2), indicates the presence of local bending adjacent to the shoulder. The tensile stresses at the shoulder are accompanied by large hoop tensile stresses of 67,447 and 78,151 psi which supports the concept of local bending adjacent to the
shoulder.
Before starting on a new optimum torque case, the connections of the test configuration were broke-out. The break-out torques are as follows:
\begin{tabular}{ccc} 
Optimum Torque & \begin{tabular}{c} 
Make-up Torque \\
ft-1b
\end{tabular} & \begin{tabular}{c} 
Break-out Torque \\
ft-1b
\end{tabular} \\
60 & 28,274 & \\
80 & 37,699 & 28,903 \\
100 & 47,124 & 47,699 \\
& & 47,752
\end{tabular}
for 100 - 102\% break-out to make-up torque.
The advance of each connection for a given torque can be found in Table B1 and Appendix B. Tabie B1 reveals consistency for the \(60 \%\), \(100 \%, 120 \%\) OTC in the advancement of the connections during make-up. In the \(80 \%\) OTC, the advancement of the connections for each torque increment falls far below those of the other optimum torque cases. The stresses in the pin, points 3 and 14, for the \(80 \%\) OTC (Table A5c, Appendix A) indicates that the torque levels of \(9,425,18,850\) and 28,274 ft-lbs should have been all the same. At this point in time, it can only be conjectured as to what happened.

The final advancement of the connections were measured at the maximum torque for the optimum torque cases relative to the \(60 \%\) OTC, and are as follows: 0.010, 0.030, \(0.048-0.050\) of a turn, respectively, for the \(80 \%, 100 \%\) and \(120 \%\) OTC. These advancements also cause the axial alignment of the strain gage on the three drilling subs of the test configuration to be further misaligned. The axial alignment of the strain gages on the three drilling subs is given in Fig. B1 of Appendix B.

\subsection*{5.3 STRESSES DUE TO AXIAL LOAD}

The average axial stress at point 8 in the tube for a \(402,025 \mathrm{lb}\). axial load is 38,610 psi, 38,550 psi, 38,985 psi and 38,665 psi, respectively, for the \(60 \%, 80 \%, 100 \%\) and \(120 \%\) OTC (Table A2c, A6c, A10c and A14c in Appendix A). The calculated axial stress in the tube of \(5-1 / 2^{\prime \prime} 0 D \times\) 4-1/8" ID cross section for 402,205 1b. axial load, is 38,678 psi which is in good agreement with stress values cited above.

Locations of high stress in the test configuration due to an axial load are at points \(1,4,5,12,15\) and 16 , which are at the transition from tube to hub in the drilling subs, as shown in Fig. 1. Listing the points in descending order of stress values is as follows: 12, 5, 16, 1, 15 and 4 , for the \(60 \%\) and \(80 \%\) OTC and \(12,5,16,15,1\) and 4 for the \(100 \%\) and \(120 \%\) OTC. The stress at these points for an axial load of 402,025 1b. compared to the stress in the tube at point 8 is as follows: 1.17 - 1.40 for point 12, \(1.16-1.17\) for point \(5,1.16\) for point 16, 1.13 for point \(15,1.12\) for point 1 and \(1.09-1.10\) for point 4.

Table 3 shows the average axial stress in the stress relief groove of the connectors for axial load increments and for the optimum torque cases. There is reasonable agreement in stress values between the optimum torque cases for a given axial load with the exception of the \(120 \%\) OTC. No reason can be offered for the slightly higher stresses in the 120\% OTC.

Figure 6 shows a plot of the average axial stress values in Table 3 for the \(120 \%\) OTC. Figure 7 is a plot of average hoop stress corresponding to the axial stress of Fig. 6. Both plots are nearly linear and both show a slight difference in stress between the two connections of the test configuration.

Comparing the average axial stress values in Table 3 for an axial load of \(402,025 \mathrm{lb}\). with the calculated axial stress value of \(15,942 \mathrm{psi}\) (Table 1) for an axial load of 400,000 shows the axial stress to be 1.07 - 1.29 greater.

Table 4 and 5 gives the axial stress in the stress relief groove of the connector for axial load increments and for odd and even numbered gages. Odd numbered gages are located on the top of the test configuration and in a vertical plane containing the axis of symmetry of the configuration. Even numbered gages are diametrically opposite the odd numbered gages. The stress values in these tables show a difference in axial stress between odd and even numbered gages. This difference is attributable to the characteristics of the loading frame not being able to apply a pure axial load to the test configuration. The actual loading imparted to the test configuration is an uniform axial load with a superimposed bending moment, therefore, the true axial stress in the test configuration should be the average axial stress. This concept is supported by comparing the average axial stress values of \(38,610,38,580,38,653 \mathrm{psi}\) for point 8 on the tube section and an axial load of \(402,025 \mathrm{lb}\). with the calculated axial stress of 38,678 psi for the same tube section and axial load. The average axial stress values are from Tables A2c, A6c, A10c and A14c in Appendix A and show good agreement with the calculated value.

\subsection*{5.4 STRESSES DUE TO BENDING LOAD}

Tables 4 and 5 also give the axial stress in the stress relief groove of the connection for bending load increments and for odd and even numbered gages. Once again, there are differences in the absolute values of the axial stress between odd and even numbered gages. These differences are assumed to be caused by the position of the chain-link loading strap on the hubs of the drilling sub relative to the pin of the connection, see Fig. 1., and the characteristics of the connection to transmit the bendinq moment. These assumptions are supported by the fact that at the center of the test configuration, point 8 , the difference in the absolute values of the stress for the odd and even gages, is negligible, less than \(2 \%\) difference. This can be verified with reference to Tables A3a, A3b, A7a, A7b, A1la, A11b, A15a and A15b in Appendix A.

The loading arrangement used to apply the bending moment to the test configuration was chosen to simulate the conditions which the drilling subs see when they come into contact with the horn on a drilling ship.

Figures 8 and 10 show plots fior the bending data given in Tables 4 and 5 , respectively. The plots show that the axial stress in the stress relief groove at point 3 and point 14 have the same characteristic trends, but with increasing separation of the curves for increasing bending moment.

Figures 9 and 11 show plots of the hoop stress which accompanies the axial stress at the stress relief groove of the connection during bending. The differences seen in the plots is assumed to be attributable to the reasons cited above.

The maximum stress in the test configuration occurs at point 12 for the even numbered gages and a bend moment of \(301,425-1 \mathrm{~b}\). The stress at point 12 is \(1.18-1.19\) greater than the stress at point 8 in the tube at the center of the test configuration. This can be verified with reference to Tables A3b, A7b, Allb and A15b in Appendix A. The next highest stress occurs at point 5 and is 1.16-1.17 greater than the stress at point 8.

\subsection*{5.5 STRESSES DUE TO COMBINED AXIAL AND BENDING LOAD}

Tables 4 and 5 also give the axial stress in the stress relief groove of the connection for the combined loading increments for odd and even numbered gages and for the \(120 \%\) OTC. The axial stress for the combined loading of \(402,025 \mathrm{lb}\). axial load and an equivalent bending moment to bend the test configuration to \(16^{\circ} / 100 \mathrm{ft}\). is the last entry in the combined load section of Tables 4 and 5 . The axial stress values from Table 5 are within +1957 psi and -4029 psi of the calculated value of 207,047 psi (Table 1) for the combined load.

When using the data in the combined load section, keep in mind that the bending moment represent the applied moment and has not been corrected for the moment due to the axial force. This would especially be true if the principle of superposition was to be used on the axial load and bending load data.

The maximum stress is at point 12 and is greater than the stress at point 8 in the tube at the center of the configuration as follows: 1.43, \(1.33,1.45\) and 1.45 respectively, for the \(60 \%, 80 \%\), \(100 \%\) and \(120 \%\) OTC. This can be verified by the data given in Tables A4b, A8b, A12b and A16b of Appendix A.

Table 6 shows the axial stress in the stress relief groove of the connection for combined make-up torque and axial load and combined make-up torque, axial and bending loads. The Table shows that the axial stress for the \(100 \%\) and \(120 \%\) OTC is greater than 136,000 psi. The yield strength for the drilling sub material is \(128,000-133,000\) psi. Therefore, for the \(100 \%\) and \(120 \%\) OTC the portion of the connection at the stress relief groove has yielded.

The high axial stress in the stress relief groove of the connection is due mainly to the make-up stress. Therefore, this stress can be lower considerably by lowering the make-up torque. If the calculated value for the stress in the stress relief groove of 67,726 psi is a goal to be achieved, then Fig. 4 shows that a make-up torque of approximately 27,000 ft-1b is required. Acceptance of lowering the make-up torque would require additional testing to verify the test results of this investigation.

At no time during the loading of the test configuration did the shoulders of the connection separate.

TABLE 1 CALCULATED AXIAL STRESSES
\begin{tabular}{|c|c|c|c|c|c|}
\hline TORQUE & AXIAL LOAD & \multicolumn{4}{|c|}{COINECTION} \\
\hline FT-LB & LB & IN-LB & PSI & PSI & \\
\hline 47124* & 0 & 0 & 67723 & & - 96708 \\
\hline 53247** & 0 & 0 & 76726 & & -109563 \\
\hline 0 & 400000 & - & 15942 & & - \\
\hline 0 & 400000 & \(16^{\circ} / 100 \mathrm{ft}\) & 27047 & & - \\
\hline 53247 & 400000 & \(16^{\circ} / 100 \mathrm{ft}\) & 105626 & & - \\
\hline
\end{tabular}
*Optimum Torque Used In This Report
**Corrected Optimum Torque

TABLE 2 AVERAGE AXIAL STRESS AT STRESS RELIEF GROOVE OF CONNECTION DUE TO MAKE-UP

AXIAL STRESS - PSI, FOR POINT LOCATION ON SPECIMEN
\begin{tabular}{llllllll} 
TORQUE \\
FT-LBS & \(3(1)\) & \(14(1)\) & \(3(2)\) & \(14(2)\) & \(3(3)\) & \(14(3)\) & \(3(4)\) \\
\(14(4)\)
\end{tabular}

\begin{tabular}{rcccccccc}
\(28275(1)\) & 71229 & 80578 & 77037 & 78682 & 70645 & 74436 & 70343 & 71881 \\
\(37699(2)\) & - & - & 91770 & 89552 & 94736 & 101314 & 95380 & 98578 \\
\(47124(3)\) & - & - & - & - & 101580 & 107047 & 119240 & 122854 \\
\(56549^{(4)}\) & - & - & - & - & - & - & 136850 & 139991
\end{tabular}
(1) 60\% Optimum Torque Case
(2) \(80 \%\) Optimum Torque Case
(3) 100\% Optimum Torque Case
(4) 120\% Optimum Torque Case

TABLE 3 AVERAGE AXIAL STRESS AT STRESS RELIEF GROOVE OF CONNECTION DUE TO AXIAL LOAD
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline AXIAL & \multirow[t]{2}{*}{\[
\begin{aligned}
& \text { BENDING } \\
& \text { LOAD } \\
& \text { IN-LBS }
\end{aligned}
\]} & \multicolumn{2}{|r|}{AVERAGE AXIAL} & STRESS & PSI, F & & \multirow[t]{2}{*}{LOCATION OR} & \multicolumn{2}{|l|}{SPECIMEN} \\
\hline \[
\begin{aligned}
& \text { LOAD } \\
& \text { LBS }
\end{aligned}
\] & & \(3(1)\) & 14 (1) & \(3(2)\) & \(14(2)\) & \(3^{(3)}\) & & \(3{ }^{(4)}\) & \(14^{(4)}\) \\
\hline 151876 & 0 & 6053 & 6008 & 6153 & 6157 & 6160 & 6420 & 6748 & 7396 \\
\hline 201013 & O & 8278 & 8169 & 8050 & 8092 & 8171 & 8377 & 8936 & 9672 \\
\hline 299286 & 0 & 12918 & 12776 & 12638 & 12809 & 12946 & 13568 & 13998 & 15104 \\
\hline 402025 & 0 & 17339 & 17128 & 16690 & 17077 & 17059 & 18082 & 19304 & 20613 \\
\hline
\end{tabular}
(1) 60\% Optimum Torque Case
(2) \(80 \%\) Opt imum Torque Case
(3) 100\% Optimum Torque Case
(4) 120\% Optimum Torque Case

TABLE 4 AXIAL STRESS AT STRESS RELIEF GROOVE OF CONNECTION DUE TO AXIAL, BENDING AND COMBINED AXIAL AND BENDING LOAD - OOD GAGES
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{\begin{tabular}{l}
AXIAL \\
LOAD \\
LBS
\end{tabular}} & \multirow[t]{2}{*}{\[
\begin{aligned}
& \text { BENDING } \\
& \text { LOAD } \\
& \text { IN-LBS }
\end{aligned}
\]} & \multirow[b]{2}{*}{3 (1)} & \multicolumn{7}{|l|}{AXIAL STRESS - PSI, FOR POINT LOCATJON ON SPECIMEN} \\
\hline & & & 14(1) & \(3(2)\) & \(14(2)\) & \(3^{(3)}\) & \(14(3)\) & \(3{ }^{(4)}\) & \(14^{(4)}\) \\
\hline 151876 & 0 & 6214 & 6412 & 6396 & 6511 & 6254 & 6803 & 6676 & 6940 \\
\hline 201013 & 0 & 8466 & 8578 & 8298 & 8479 & 8275 & 8766 & 8753 & 8894 \\
\hline 299286 & 0 & 13118 & 13319 & 12979 & 13361 & 13127 & 14093 & 13569 & 13500 \\
\hline 402025 & 0 & 17555 & 17726 & 17113 & 17759 & 17407 & 18755 & 18643 & 18171 \\
\hline 0 & 43304 & -1266 & -1052 & -1332 & -1226 & -1180 & -1193 & -1058 & -1098 \\
\hline 0 & 146552 & -2690 & -2502 & -2674 & -2809 & -2561 & -2786 & -2261 & -2446 \\
\hline 0 & 198177 & -4005 & -3798 & -4019 & -4256 & -3666 & -4012 & -3333 & -3841 \\
\hline 0 & 249801 & -5156 & -4985 & -5070 & -5492 & -4882 & -5482 & -4404 & -5136 \\
\hline 0 & 301425 & -6303 & -6102 & -6250 & -6761 & -6063 & -6798 & -5433 & -6461 \\
\hline 402025 & 43304 & 16457 & 16694 & 16757 & 17123 & 17321 & 17548 & 17416 & 17202 \\
\hline 402025 & 146552 & 16038 & 16352 & 16236 & 16582 & 16823 & 17027 & 17163 & 16991 \\
\hline 402025 & 198177 & 15663 & 15976 & 15850 & 16259 & 16503 & 16629 & 16810 & 16526 \\
\hline 402025 & 249801 & 15310 & 15633 & 15540 & 15864 & 16061 & 16154 & 16444 & 16216 \\
\hline 402025 & 301425 & 14769 & 15168 & 15175 & 15531 & 15643 & 15778 & 16134 & 15860 \\
\hline 402025 & 507922 & 13312 & 13642: & - & -- & - & - & - & - \\
\hline 402025 & 559546 & - & - & 13098 & 13187 & 13556 & 13411 & 14387 & 13474 \\
\hline 402025 & 827992 & 9831 & 9837 & - & - & - & - & - & - \\
\hline 402025 & 920916 & - & - & - & - & 10375 & 9738 & - & - \\
\hline 402025 & 941566 & - & - & - & - & - & - & 11515 & 24420 \\
\hline 402025 & 951891 & - & - & 9827 & 9646 & - & - & - & - \\
\hline
\end{tabular}
(1) 60\% Optimum Toroue Case
2) \(80 \%\) Optimum Torque Case
(3) \(100 \%\) Optimum Torque Case
(4) \(120 \%\) Opt imum Torque Case

TABLE 5 AXIAL STRESS AT STRESS RELJEF GRODVE OF CONNECTION DUE TO AXIAL, BENDING AND COMBINED AXIAL AND BENDING LOAD - EVEN GAGES
\begin{tabular}{llllllllll} 
AXIR: & BENDING & & AXIAL STRESS - PSI, FOR POINT LOCATION ON SPECIMEN \\
LOAT & LOAD & & \(3(1)\) & \(14(1)\) & \(3(2)\) & \(14(2)\) & \(3(3)\) & \(14(3)\) & \(3(4)\) \\
LBS & IN-LBS & \(3(4)\) & \(14(4)\)
\end{tabular}
\begin{tabular}{rrrrrrrrrr}
151876 & 0 & 5891 & 5604 & 5911 & 5802 & 6066 & 6033 & 6821 & 7853 \\
201013 & 0 & 8090 & 7760 & 7803 & 7704 & 8067 & 7988 & 9119 & 10450 \\
299786 & 0 & 12719 & 12234 & 12297 & 12257 & 12765 & 13042 & 14426 & 16708 \\
402025 & 0 & 17123 & 16530 & 16266 & 16394 & 16711 & 17410 & 19965 & 23054 \\
0 & 43304 & 976 & 1160 & 966 & 1098 & 976 & 1164 & 916 & 1246 \\
0 & 146552 & 2357 & 2825 & 2509 & 2743 & 2324 & 2723 & 1938 & 2650 \\
0 & 198177 & 3781 & 4272 & 3758 & 4114 & 3485 & 3972 & 3043 & 4022 \\
0 & 249801 & 5018 & 5588 & 4919 & 5255 & 4645 & 5288 & 4190 & 5459 \\
0 & 301425 & 6069 & 6781 & 5937 & 6465 & 5759 & 6570 & 5153 & 6705 \\
402025 & 433304 & 16777 & 16141 & 16879 & 16619 & 16971 & 16942 & 18389 & 18135 \\
402025 & 146552 & 17054 & 16450 & 17265 & 17093 & 17390 & 17350 & 18587 & 18369 \\
402025 & 198177 & 17407 & 16780 & 17618 & 17426 & 17776 & 17726 & 18930 & 18821 \\
402025 & 249801 & 17726 & 17080 & 17960 & 17789 & 13010 & 18036 & 19282 & 19243 \\
402025 & 301425 & 18158 & 17499 & 18290 & 18155 & 18287 & 18402 & 19635 & 19694 \\
402025 & 507922 & 19540 & 19015 & - & - & - & - & - & - \\
402025 & 559546 & - & - & 20423 & 20631 & 20344 & 21231 & 21900 & 22783 \\
402025 & 827992 & 23238 & 23018 & - & - & - & - & - & - \\
402025 & 920916 & - & - & - & - & 23644 & 26123 & - & - \\
402025 & 941566 & - & - & - & - & - & - & 26245 & 29004 \\
402025 & 951891 & - & - & 23927 & 24804 & - & - & - & -
\end{tabular}
(1) 60\% Optimum Torque Case
(2) \(80 \%\) Optimum Torque Case
(3) 100\% Optimum Torque Case
(4) 120\% Optimum Torque Case

TABLE 6 AXIAL STRESS AT STRESS RELIEF GROOVE OF CONNECTION DUE TO CONBJHED LOADING
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline OPTIMU: TORQUE & CASE & \[
\begin{aligned}
& \text { TORQUE } \\
& \text { FT-LB }
\end{aligned}
\] & \[
\underset{L B}{A X I A L}
\] & \[
\begin{gathered}
\text { BENDING LOAD } \\
\text { IN-LB }
\end{gathered}
\] & \multicolumn{2}{|l|}{AXIAL STRESS PS1} \\
\hline & 60 & 28274 & 402025 & 0 & 85861 & 79083 \\
\hline & 60 & 28274 & 402025 & 827992 & 91760 & 84972 \\
\hline & 80 & 37699 & 402025 & 0 & 112070 & 115655 \\
\hline & 80 & 37699 & 402025 & 951897 & 119307 & 123382 \\
\hline & 100 & 47124 & 402025 & 0 & 136299 & 140937 \\
\hline & 100 & 47124 & 402025 & 920916 & 142884 & 148978 \\
\hline & 120 & 56549 & 402025 & 0 & 156158 & 160604 \\
\hline & 120 & 56549 & 402025 & 941566 & 163099 & 168995 \\
\hline
\end{tabular}

NOTE:
1. Numbers represent point numbers of gage locations on test configuration.
2. Make-up stresses are from Table A13c, Appendix A.
3. Axial stress values for axial and bending load are from Tables \(A A C, A B C\), A12C and A16C in Appendix A, respectively for the \(60 \%, 80 \%, 100 \%\) and \(120 \%\) optimum torque case.

\begin{tabular}{|c|l|}
\hline ITEM & \multicolumn{1}{|c|}{ DESCRIPTION } \\
\hline A & HORIZONTAL FRAME AND END MEMBERS \\
\hline B & UPPER FRAME \\
\hline C & TEST CONFIGURATION \\
\hline D & PULLING ADAPTERS \\
\hline E & FIXED BEARING SUPPORT \\
\hline F & HORIZONTAL SUPPORT \\
\hline G & HYDRAULIC CYLINDER (AXIAL LOAD) \\
\hline H & CHAIN-LINK STRAPS \\
\hline I & LOADING BEAM \\
\hline J & HYDRAULIC CYLINDER (BENDING LOAD) \\
\hline
\end{tabular}

FIG. 1 TEST FRAME \& SPECIMEN CONFIGURATION

a) Make-up Mode

b) Bending or Combined Axial and Bending Mode


NOTES: I) ALL STRAIN LOCATIONS CONSIST OF SINGLE ELEMENT GAGES ORIENTED IN THE AXIAL DIRECTION.
2) ENCIRCLED NUMBERS REPRESENT POINT LOCATION OF GAGES.
\(\because-90^{\circ}\) STRAIN ROSETTE
\# - AXIAL STRAIN \& FATIGUE GAGE

FIG. 3 STRAIN GAGE LOCATIONS


FIG. 4 AVERAGE AXIAL STRESS AT STRESS RELIEF GROOVE OF CONNECTION DUE TO MAKE-UP \((120 \%\) OPTIMUM TORQUE CASE)


FIG. 5 AVERAGE HOOP STRESS AT STRESS RELIEF GROOVE OF
CONNECTION DUE TO MAKE-UP (I20\% OPTIMUM TORQUE CASE)



FIG. 7 AVERAGE HOOP STRESS AT STRESS RELIEF GROOVE OF CONNECTION DUE TO AXIAL LOAD (I20\% OPTIMUM TORQUE CASE)



FIG. 9 HIOOP STRESS AT STRESS RELIEF GROOVE OF CONNECTION DUE. TO BENDING LOAD-ODD GAGES-(120\% OPTIMUM TORQUE CASE)



Appendix \(A\) has been omitted in the interest of brevity. It contains the data from all the strain gages used during the experimental evaluation, and can be found in Reference 5.

\section*{APPENDIX B}

Connection Rotation For 60\%, 80\%, 100\% And 120\% Optimum Torque Cases


FIG. BI STRAIN GAGE ALIGNMENT AT 60\% OPTIMUM TORQUE CASE

TABLE BI CONNECTION ROTATION DURING MAKE-UP

TURNS, FOR \(5-1 / 2^{\prime \prime}\) 1.F. CONNECTION
\begin{tabular}{|c|c|c|c|c|c|c|c|c|}
\hline \[
\begin{aligned}
& \text { TORQUE } \\
& \text { FT-LBS }
\end{aligned}
\] & \(\mathrm{LEFT}^{(1)}\) & RIGHT \({ }^{(1)}\) & \[
\begin{array}{r}
\text { TURNS } \\
\text { LEFT }^{(2)}
\end{array}
\] & \[
\begin{aligned}
& \text { FOR } 5-1 / 2 \\
& \text { RIGHT }^{(2)}
\end{aligned}
\] & \[
\begin{aligned}
& \text { 1.F. CO } \\
& \text { LEFT }^{(3)}
\end{aligned}
\] & \[
\begin{aligned}
& \text { ECTION } \\
& \text { RIGHT }^{(3)}
\end{aligned}
\] & LEFT \(^{(4)}\) & R1GH7 \({ }^{(4)}\) \\
\hline HAND TIGHT & - & - & - & - & 0.000 & 0.000 & 0.000 & 0.000 \\
\hline 9425 & 0.000 & 0.000 & 0.000 & 0.000 & 0.060 & 0.070 & 0.008 & 0.015 \\
\hline 18850 & 0.020 & 0.025 & 0.000 & 0.001 & 0.085 & 0.090 & 0.028 & 0.035 \\
\hline 28274(1) & 0.040 & 0.045 & 0.000 & 0.002 & 0.103 & 0.105 & 0.048 & 0.050 \\
\hline \(37699^{(2)}\) & - & - & 0.010 & 0.012 & 0.113 & 0.122 & 0.063 & 0.065 \\
\hline 47124 \({ }^{(3)}\) & - & - & - & - & 0.130 & 0.140 & 0.078 & 0.082 \\
\hline \(56544^{(4)}\) & - & - & - & - & 0.130 & 0.1 & 0.096 & 0.100 \\
\hline \begin{tabular}{l}
CAL CULATED ADVANCE \\
FROM 28274
\end{tabular} & & & & & & & & \\
\hline FT-LB REF. & 0.000 & 0.000 & - & - & 0.030 & 0.025 & 0.048 & 0.040 \\
\hline MEASURED & & & & & & & & \\
\hline \begin{tabular}{l}
ADVANCE \\
FROM 28274
\end{tabular} & & & & & & & & \\
\hline FT-LB REF. & - & - & 0.010 & 0.010 & 0.030 & 0.030 & 0.048 & 0.050 \\
\hline
\end{tabular}
(1) 60: Optimum Torque Case
(2) \(80 \%\) Optimum Torque Case
(3) 100\% Optimum Torque Case
(4) 120: Optimum Torque Case

\section*{APPENDIX C}

Bending Deflections For 60\%, 80\%, 100\% And 120\% Optimum Torque Cases

\section*{LIST OF TABLES}

Table

C1
C2
C3
C4

Bending Deflection For 60\% Optimum Torque Case Bending Deflection For \(80 \%\) Optimum Torque Case Bending Deflection For 100\% Optimum Torque Case Bending Deflection For 120\% Optimum Torque Case


FIG. CI DIAL INDICATOR LOCATIONS

TABLE CI BENDING DEFLECTIONS FOR 60\% OPTIMUM TORQUE CASE
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline \multirow[t]{2}{*}{\begin{tabular}{l}
AXIAL \\
LOAD
\end{tabular}} & BENDING & \multicolumn{5}{|c|}{DIAL INDICATOR READINGS (INCHES)} \\
\hline & \multicolumn{6}{|l|}{LOAD} \\
\hline LB. & IN-LB & A & B & C & D & E \\
\hline & & & & & & \\
\hline & & & & & & \\
\hline 0 & 43304. & 0.205 & 0.223 & 0.224 & 0.223 & 0.302 \\
\hline 0 & 146552 & 0.471 & 0.520 & 0.525 & 0.520 & 0.472 \\
\hline 0 & 198177 & 0.510 & 0.782 & 0.790 & 0.783 & 0.707 \\
\hline 0 & 249801 & 0.927 & 1.020 & 1.032 & 1.021 & 0.926 \\
\hline 0 & 301425 & 1.142 & 1.256 & 1.272 & 1.258 & 1.137 \\
\hline 402025 & 43304 & 0.053 & 0.055 & 0.056 & 0.054 & 0.047 \\
\hline 402025 & 146552 & 0.092 & 0.100 & 0.099 & 0.097 & 0.081 \\
\hline 402025 & 198177 & 0.140 & 0.150 & 0.148 & 0.144 & 0.121 \\
\hline 402025 & 249801 & 0.180 & 0.195 & 0.194 & 0.188 & 0.159 \\
\hline 402025 & 301425 & 0.254 & 0.271 & 0.268 & 0.260 & 0.220 \\
\hline 402025 & 507922 & 0.445 & 0.485 & 0.486 & 0.478 & 0.419 \\
\hline 402025 & 827992 & 1.020 & 1.123 & 1.132 & 1.120 & 1.072 \\
\hline
\end{tabular}

TABLE C2 BENDING DEFLECTION FOR 80\% OPTIMUM TORQUE CASE
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline AXIAL & BENDING & \multicolumn{5}{|c|}{\multirow[t]{2}{*}{DIAL INDICATOR READINGS (INCHES)}} \\
\hline LOAD & LOAD IN-LB & & & & & \\
\hline & & & & & & \\
\hline 0 & 43304. & 0.205 & 0.129 & 0.231 & 0.229 & 0.105 \\
\hline 0 & 146552 & 0.488 & 0.439 & 0.544 & 0.539 & 0.385 \\
\hline 0 & 198177 & 0.744 & 0.719 & 0.827 & 0.818 & 0.635 \\
\hline 0 & 249801 & 0.957 & 0.953 & 1.064 & 1.050 & 0.846 \\
\hline 0 & 301425 & 1.170 & 1.196 & 1.300 & 1.283 & 1.055 \\
\hline 402025 & 43304 & 0.049 & 0.052 & 0.053 & 0.050 & 0.043 \\
\hline 402025 & 146552 & 0.108 & 0.117 & 0.124 & 0.113 & 0.093 \\
\hline 402025 & 198177 & 0.155 & 0.168 & 0.165 & 0.161 & 0.135 \\
\hline 402025 & 249801 & 0.201 & 0.217 & 0.215 & 0.209 & 0.176 \\
\hline 402025 & 301425 & 0.251 & 0.271 & 0.268 & 0.261 & 0.220 \\
\hline 402025 & 559546 & 0.600 & 0.650 & 0.649 & 0.638 & 0.555 \\
\hline 402025 & 951891 & 1.182 & 1.289 & 1.294 & 1.275 & 1.133 \\
\hline
\end{tabular}

TABLE C3 BENDING DEFLECTION FOR 100\% OPTIMUM TORQUE CASE
\begin{tabular}{|c|c|c|c|c|c|c|}
\hline AXIAL & BENDING & \multicolumn{5}{|c|}{DIAL INDICATOR READINGS (INCHES)} \\
\hline LOAD & LOAD & \multirow[b]{2}{*}{A} & & & \multirow[b]{2}{*}{D} & \multirow[b]{2}{*}{E} \\
\hline LB' & IN-LB & & B & C & & \\
\hline 0 & 43304 & 0.210 & 0.230 & 0.232 & 0.229 & 0.208 \\
\hline 0 & 146552 & 0.483 & 0.532 & 0.536 & 0.531 & 0.480 \\
\hline 0 & 198177 & 0.696 & 0.767 & 0.775 & 0.766 & 0.694 \\
\hline 0 & 249801 & 0.926 & 1.021 & 1.031 & 1.019 & 0.925 \\
\hline 0 & 301425 & 1.144 & 1.261 & 1.274 & 1.259 & 1.142 \\
\hline 402025 & 43304 & 0.043 & 0.046 & 0.046 & 0.045 & 0.036 \\
\hline 402025 & - 146552 & 0.105 & 0.114 & 0.113 & 0.110 & 0.090 \\
\hline 402025 & 198177 & 0.157 & 0.170 & 0.168 & 0.164 & 0.137 \\
\hline 402025 & 249801 & 0.208 & 0.225 & 0.223 & 0.216 & 0.182 \\
\hline 402025 & 301425 & 0.261 & 0.283 & 0.279 & 0.272 & 0.230 \\
\hline 402025 & 559546 & 0.620 & 0.674 & 0.675 & 0.660 & 0.580 \\
\hline 402025 & 920916 & 1.184 & 1.299 & 1.307 & 1.289 & 1.153 \\
\hline
\end{tabular}

TABLE C4 BENDING DEFLECTION FOR 120\% OPTIMUM TORQUE CASE


\section*{APPENDIX D}

Sample Calculations For 5-1/2"I.F. Connection For 7-3/4" OD X 4-1/8" ID Drilling Sub By Dr. P. D. Weiner

5-1/2 inch I.F. connection with a 7-3/4 inch outside diameter and 4-1/8 inch inside diameter.

Box Moment of Inertia
\[
I_{B}=\pi / 64\left(7.75^{4}-5.8^{4}\right)
\]

Pin Moment of Inertia
\[
\begin{aligned}
I_{P} & =\pi / 64 \text { (5.8.9 } \\
& =44.87 \text { in } 4
\end{aligned}
\]

Ratio of Moment of Inertia
\[
\begin{aligned}
I_{B / I_{P}} & =\frac{121.53}{44.87} \\
& =2.71
\end{aligned}
\]

Box Section Modulus
\[
\begin{aligned}
Z & =\frac{\pi / 64\left(7.75^{4}-5.8^{4}\right)}{7.75} \\
& =15.68 \mathrm{in}^{3}
\end{aligned}
\]

Pin Section Modulus
\[
\begin{aligned}
z_{\mathrm{P}} & =\frac{\pi / 645.89^{4}-4.125^{4}}{5.89} \\
& =7.62 \mathrm{in}^{3}
\end{aligned}
\]

Bending Strength Ratio
\[
\begin{aligned}
B S R & =z \\
& =\frac{15}{B / Z P} \\
& =2.62 \\
& 2.06
\end{aligned}
\]

Box Area
\[
\begin{aligned}
A_{B} & =\frac{\pi}{4}\left(7.75^{2}-5.8^{2}\right) \\
& =20.75 \mathrm{in}^{2}
\end{aligned}
\]

Pin Area
\[
\begin{aligned}
A_{P} & =\frac{\pi}{4}\left(5.89^{2}-4.125^{2}\right) \\
& =13.88 \mathrm{in}^{2}
\end{aligned}
\]

Area Ratio
\[
\begin{aligned}
A_{R} & =\frac{A_{B}}{A_{P}} \\
& =\frac{20.75}{13.88} \\
& =1.5
\end{aligned}
\]

Box Area at Recess
\[
\begin{aligned}
A_{\text {Recess }} & =\frac{\pi}{4}\left(7.75^{2}-6.453^{2)}\right. \\
& =14.46 \mathrm{in}^{2}
\end{aligned}
\]

Box Contact Area
\[
\begin{aligned}
{ }^{A_{\text {Contact }}} & =\frac{\pi}{4}\left(7.35^{2}-6.453^{2}\right) \\
& =9.72 \mathrm{in}^{2}
\end{aligned}
\]

Moment of Inertia Main Beam
\[
\begin{aligned}
I & =\frac{\pi}{64}\left(7.75^{4}-6.453^{4}\right) \\
& =91.97 \mathrm{in}^{4}
\end{aligned}
\]

Moment of Inertia Box in Compression
\[
\begin{aligned}
I_{1} & =\frac{\pi}{64}\left[7.35^{4}-6.453^{4}\right] \\
& =54.29 \text { in }^{4}
\end{aligned}
\]

Make-Up Torque
\(T=\frac{C_{1} E A}{12}\)\(\left[Q_{C}+26\right]\left[\frac{I}{I_{1}}\right]\left[\frac{P}{2}+\frac{R_{t} f}{\cos t}+R_{s} f\right]\)
Where \(P=.25\) inches \(/\) thread
\[
\begin{aligned}
R_{t} & =\frac{C+D_{s}-H}{4} \\
& =\frac{6.189+5.564-0.216}{4} \\
& =2.992 \mathrm{in} \\
R_{S} & =\frac{D+Q_{C}}{4} \\
& =\frac{7.75+6.453}{4} \\
& =3.55 \mathrm{in} . \\
Q_{C}+ & =60=6.453+(2)(0.2) \\
& =6.853 \text { in } \\
C_{1} & =2.203 \times 10^{-4} \text { for } 160 \text { deflection per } 100 \text { feet } \\
{\left[\begin{array}{rl}
P
\end{array}\right.} & \left.\left.+R_{t} F+R_{s} F\right]=\frac{.25}{2}+\frac{(2.99)(.08)}{300}+(3.55)(.08)\right] \\
& =.04+.276+.284 \\
& =0.6
\end{aligned}
\]
```

Torque $=\left(2.203 \times 10^{-4}\right)\left(30 \times 10^{6}\right)(13.88)(6.853)(91.97)(0.6)$
$=53247 \mathrm{ft}-\#$

```

Force Due to Torque
\[
\begin{aligned}
F_{i} & =\frac{(T)(12)}{P / 2 \pi+R_{t} F}+R_{s} F \\
& =\frac{(53247)(12)}{\operatorname{Cos} t} \\
& =1,064,957 \#
\end{aligned}
\]

Shoulder Stress
\[
\begin{aligned}
\mathbf{S}_{\text {shoulder }} & =\frac{1,064,957}{9.72} \\
& =109563 \mathrm{psi}
\end{aligned}
\]

Pin Stress
\[
S_{p}=\frac{F_{i}}{A_{p l}}
\]
\[
\begin{aligned}
\text { Spin } & =\frac{1,064,957}{13.88} \\
& =76,726 \mathrm{psi}
\end{aligned}
\]

Stress in Box
\[
\begin{aligned}
S_{B i} & =F_{i} \\
& =\frac{1,064,957}{A_{B}} \\
& =51,323
\end{aligned}
\]

Box Shoulder Stress
\[
\begin{aligned}
\mathrm{S}_{\mathrm{Bsi}} & =\frac{1,064,957}{9.72} \\
& =109,563 \mathrm{psi}
\end{aligned}
\]

Opening Force
\[
\begin{aligned}
F_{o} & =F_{i}\left[\begin{array}{|c}
\frac{A_{p}}{A_{B}}+A_{B} \\
\\
\end{array}\right]=1,064,957\left[\frac{13.88+(14.46+9.72)(.5)}{(14.46+9.72)(.5)}\right]
\end{aligned}
\]
\[
F_{o}=2,287,586 \mathrm{lbs}
\]

Change in Pin Load
\[
\Delta F_{p}=F_{e}\left[\frac{A_{p}}{A_{B}+A p}\right]
\]
\[
\text { For } \mathrm{F}_{\mathrm{e}}=400,000 \mathrm{lbs}
\]

Change in force on the pin
\(\Delta F_{p}=(.55)(400000)\)
\(\mathrm{p}=221,283 \mathrm{lbs}\)
Then the total force on the pin is
\[
\begin{aligned}
F_{\text {pin total }} & =F_{i}+F_{p} \\
& =1,064,957+221,283 \\
& =1,286,240 \text { lbs }
\end{aligned}
\]

The resulting stress
\[
\begin{aligned}
\mathrm{S}_{\text {pin }} & =\frac{1,286,240}{13.88} \\
& =92,668 \mathrm{psi}
\end{aligned}
\]
or change in Pin Stress
1) \(\mathrm{S}_{\mathrm{pin}_{\mathrm{A}}}=\frac{221,203}{13.88}\)
\[
=15,942 \mathrm{psi}
\]

Bending effect
\[
\begin{aligned}
S_{\text {Bending }} & =218.125 \mathrm{D} \text { per } 0 / 100 \text { feet } \\
\text { or } & =3490 \mathrm{D} \text { for } 160 / 100 \text { feet } \\
\text { The } \mathrm{S}_{\text {Bending }} & =(3490)(7.75) \\
& =27047 \mathrm{psi}
\end{aligned}
\]

If we consider this as an external force
\[
\text { in } S=\frac{F}{\overline{A B}}
\]
\[
\mathrm{F}_{\mathrm{e}}=(27047)(12.09)
\]
\[
=326,998 \mathrm{lbs}
\]
or on the tensile side of the beam
the \(\Delta F_{p_{b}}=(.55)(326,998)\)
\[
=179,849 \mathrm{lbs}
\]
or the additional stress in the pin is
\(S_{\text {pin Bending }}=\frac{179849}{13.88}\)
\[
=12957 \mathrm{psi}
\]
\[
\begin{aligned}
& \text { \& the total pin stress } \\
& S_{\text {pin total }}=S_{i}+S_{A}+S_{\text {Bending }}=76,727+15,942+12,957 \\
&=105,626 \mathrm{psi}
\end{aligned}
\]

The box compressive stress would be
\[
\begin{aligned}
S_{B} & =\frac{1,064,957-180,000-147,149}{12.09} \\
& =61,026 \mathrm{psi}
\end{aligned}
\]

\footnotetext{
5-1/2 inch full hole with 7-3/4 inch outside diameter and 4-1/8 inch inside diameter.
}

Box Member Moment of Inertia
\[
\begin{aligned}
I_{B} & =\pi 64\left[7.75^{4}-5.172^{4}\right] \\
& =141.93 \text { in }^{4}
\end{aligned}
\]

Pin Moment of Inertia
\[
\begin{aligned}
I_{p} & =\pi / 64\left[5.25^{4}-4.125^{4}\right] \\
& =23.08 \text { in } 4
\end{aligned}
\]

Ratio of Moment of Inertia
\[
\begin{aligned}
I_{B / I_{P}} & =\frac{141.93}{23.08} \\
& =6.15
\end{aligned}
\]

Box Section Modulus
\[
\begin{aligned}
z_{B} & =\frac{\pi / 64\left[7.75^{4}-5.172^{4}\right]}{7.75} \\
& =18.31
\end{aligned}
\]

Pin Section Modulus
\[
\begin{aligned}
Z_{P} & =\frac{\pi 64\left[5.25^{4}-4.125^{4}\right]}{5.25} \\
& =4.4
\end{aligned}
\]

Bending Strength Ratio
\[
\begin{aligned}
\mathrm{BSR} & =\mathrm{ZB} / \mathrm{ZP} \\
& =18.31 / 4.4 \\
& =4.16
\end{aligned}
\]

Box Area
\[
\begin{aligned}
A_{B} & =\pi 4\left[7.75^{2}-5.172^{2}\right] \\
& =26.16 \text { in }^{2}
\end{aligned}
\]

Pin Area
\[
\begin{aligned}
\mathrm{A}_{\mathrm{P}} & =\pi_{4}\left[5.25^{2}-4.125^{2}\right] \\
& =8.28 \mathrm{in} 2
\end{aligned}
\]

Area Ratio
\[
\begin{aligned}
A_{R} & =A_{B /} A_{P} \\
& =\frac{26.16}{8.28} \\
& =3.16
\end{aligned}
\]

Box Area Under Recess
\[
\begin{aligned}
\mathrm{A}_{\text {Recess }} & =\pi / 4\left[7.75^{2}-5.906^{2}\right] \\
& \left.=19.78 \mathrm{in}^{2}\right]
\end{aligned}
\]

Box Contact Area
\[
\begin{aligned}
A_{\text {contact }} & =\pi / 4\left[7.35^{2}-5.906^{2}\right] \\
& =15.03
\end{aligned}
\]

Moment of Inertia Main Beam
\[
\begin{aligned}
I & =\pi_{64}\left[7.75^{4}-5.906^{4}\right] \\
& =117.34 \mathrm{in}^{4}
\end{aligned}
\]

Moment of Inertia of the Box in Compression
\[
\begin{aligned}
I_{1} & =\pi / 64\left[7.35^{4}-5.906^{4}\right] \\
& =83.52
\end{aligned}
\]
\[
\begin{aligned}
R_{t} & =\frac{5.591+4.992}{4} \\
& =2.646 \mathrm{in}
\end{aligned}
\]
\[
\mathrm{R}_{\mathrm{S}}=\frac{7.75+5.906}{4}
\]
\[
=3.414 \mathrm{in}
\]
\[
\begin{aligned}
Q_{C}+2 \mathrm{~S} & =5.906+(2)(.2) \\
& =6.306
\end{aligned}
\]
\[
c_{1}=2.203 \times 10^{-4}
\]
\[
\left[\frac{p}{2 \pi}+\frac{R_{t f}}{\cos t}+R_{s f}\right]=\left[\frac{.25}{}+\frac{(2.646)(.08)}{\cos t 30^{\circ}}+(3.414)(.08)\right]
\]
\[
=.04+.244+.273
\]
\[
=.557
\]
\[
\begin{aligned}
T & =\frac{\left(2.203 \times 10^{-4}\right)\left(30 \times 10^{6}\right)(8.28)(6.306)(117.34)(.557)}{(12)(83.52)} \\
& =22.503 \mathrm{ft}-\#
\end{aligned}
\]

Force Due to Torque
\[
\begin{aligned}
F_{i} & =\frac{(22503(12)}{.557} \\
& =484,804 \mathrm{lbs}
\end{aligned}
\]
\[
\begin{aligned}
S_{\text {Shoulder }} & =\frac{484,804}{15.03} \\
& =32,255 \mathrm{psi}
\end{aligned}
\]

Pin Stress
\[
\begin{aligned}
\text { Spin } & =\frac{484,804}{8.28} \\
& =58,551 \mathrm{psi}
\end{aligned}
\]

Stress in the Box
\[
\begin{aligned}
\mathbf{S}_{\mathbf{B}_{\mathbf{i}}} & =\frac{484,804}{26.16} \\
& =18,532 \mathrm{psi}
\end{aligned}
\]

Box Shoulder Stress
\[
\begin{aligned}
S_{B s i} & =\frac{484,804}{15.03} \\
& =32,255 \mathrm{psi}
\end{aligned}
\]
\(\begin{aligned} & \text { Opening Force } \\ & \mathrm{F}_{\mathrm{o}}=484,804\left[\frac{8.28+(19.78+15.03)(.5)}{(19.78+15.03)(.5)}\right] \\ &=715,643 \mathrm{lbs}\end{aligned}\)
\[
=715,643 \mathrm{lbs}
\]

Change in Pin Load
\[
\begin{aligned}
\Delta \mathrm{F}_{\mathrm{p}} & =\mathrm{F}_{\mathrm{e}}\left[\frac{A_{\mathrm{p}}}{\bar{A}_{\mathrm{B}}+A_{p}}\right] \\
& =\mathrm{F}_{\mathrm{e}}\left[\begin{array}{l}
8.28 \\
17.4+8.28
\end{array}\right] \\
& =\left(\mathrm{F}_{\mathrm{e}} \mathrm{~J}(.322)\right.
\end{aligned}
\]

For \(\mathrm{F}_{\mathrm{e}}=400,000 \mathrm{lbs}\)
Change in Pin Force
\(\Delta \mathrm{F}_{\mathrm{b}}=(.322)(400,000)\)
\[
=128,972 \mathrm{lbs}
\]

The total force on the pin
\[
\begin{aligned}
\mathrm{F} \text { pin } i+\mathrm{A} & =484,804+128,972 \\
& =613,776 \mathrm{lbs}
\end{aligned}
\]

The Resulting Stress
\[
\begin{aligned}
S_{\text {pin } i}+A & =\frac{613,776}{8.28} \\
& =74,127 \mathrm{psi}
\end{aligned}
\]
or the change in pin stress
\[
\begin{aligned}
\Delta S_{\text {pin } A} & =\frac{128,972}{8.28} \\
& =15,576 \mathrm{psi}
\end{aligned}
\]

Bending Effect
\[
\begin{aligned}
\mathrm{S}_{\text {Bending }} & =3490 \mathrm{D} \\
& =(3490)(7.75) \\
& =27,047 \text { psi }
\end{aligned}
\]

If we consider this as an external force
\[
\begin{aligned}
\mathrm{Fe} & =(27,047)(17.4) \\
& =470,617 \mathrm{lbs}
\end{aligned}
\]

Or the additional tensile force on the beam
\[
\begin{aligned}
\mathrm{F}_{\mathrm{pb}} & =(.322)(470,617) \\
& =151,539 \mathrm{lbs}
\end{aligned}
\]

Or the additional stress due to bending in the pin is
\[
\Delta S_{\mathrm{pb}}=\frac{151,539}{8.28}
\]
\[
=18,302 \mathrm{psi}
\]

And the total pin stress is
\[
\begin{aligned}
S_{\text {total }} & =S_{i}+S_{A}+S_{B} \\
& =58,551+15,576+18,302 \\
& =92,429 \text { psi }
\end{aligned}
\]

The resulting box force is
\[
\begin{aligned}
\mathrm{F}_{\mathrm{B}} & =-484,804+271,028+319,078 \\
& =105,302 \quad .: \text { Box Opens }
\end{aligned}
\]

If we increase the initial pin stress to 750,000 psi
\(\mathrm{F}_{\mathrm{i}}=(8.28)(75,000)\) \(=621,000 \mathrm{lbs}\)
\[
T=\frac{(621,000)(.557)}{12}
\]
\[
=28,825 \mathrm{ft}-\#
\]

Stress in the Box
\[
\mathrm{S}_{\mathrm{Bi}}=\frac{621,000}{26.16}
\]
\[
=23,738 \mathrm{psi}
\]

Box Shoulder Stress
\[
\begin{aligned}
S_{B S i} & =\frac{621,000}{15.03} \\
& =41,317 \mathrm{psi}
\end{aligned}
\]
\(\begin{aligned} & \text { Opening Force } \\ & \mathrm{F}_{\mathrm{O}}=621,000[1.476] \\ &=916,596 \mathrm{lbs}\end{aligned}\)
\[
=916,596 \mathrm{lbs}
\]

The final force on the pin would be with 400,000 lbs axial load and 16 degrees per 100 foot bend is
\[
\begin{aligned}
\mathrm{F}_{\text {total }} & =621,000+128,972+151,539 \\
& =901,511 \mathrm{lbs} \\
\mathrm{~S}_{\text {total }} & =\frac{901,511}{8.28} \\
& =108,878 \mathrm{psi}
\end{aligned}
\]

And the final box force is
\(\mathrm{F}_{\text {Box Total }}=-621,000+271,028+319,078\)
.: The box is still in compression and the connection remains together.

Comparison between the two connections follows.
\begin{tabular}{|c|c|c|}
\hline Type & 5-1/2 inch I.F. & 5-1/2 inch F.H. \\
\hline O.D. & 7-3/4 in & \(7-3 / 4\) in \\
\hline I.D. & 4-1/8 in & 4-1/8 in \\
\hline M.O. Torque & 53,247 ft-1bs & 28,825 ft-lbs \\
\hline \(\mathrm{F}_{\mathrm{i}}\) & 1,064,957 lbs & \(621,000 \mathrm{lbs}\) \\
\hline \(\mathrm{F}_{0}\) & 2,287,586 lbs & 916,596 lbs \\
\hline \(\mathrm{I}_{\mathrm{B}}\) & 121.53 in \(^{4}\) & 141.93 in \({ }^{4}\) \\
\hline \(\mathrm{I}_{\mathrm{P}}\) & 44.87 in \(^{4}\) & 23.08 in \(^{4}\) \\
\hline \({ }^{\text {A }}\) B & 20.75 in \(^{2}\) & 26.16 in \(^{2}\) \\
\hline \(A_{\text {P }}\) & \(13.88 \mathrm{in}^{2}\) & \(8.28 \mathrm{in}^{2}\) \\
\hline \(S_{\text {pi }}\) & 76,726 psi & 75,000 psi \\
\hline \(\mathrm{S}_{\mathrm{Bi}}\) & -109,563 psi & -41,317 psi \\
\hline \(\mathrm{S}_{\text {PTotal }}\) & 105,626 psi & 108,878 psi \\
\hline \(\mathrm{S}_{\text {BTotal }}\) & -61,026 psi & -2,055 psi \\
\hline \[
I_{B /} I_{P}
\] & 2.71 & 6.15 \\
\hline BSR & 2.06 & 4.16 \\
\hline \(\mathrm{F}_{\mathrm{p}}\) & . 55 Fe lbs & . 322 Fe lbs \\
\hline
\end{tabular}

The above comparison shows that the I.F connection is better than the FH connection for the type of loading that this drill string will be receiving that is a combination of tension and bending in that since the pin will be subjected to large tensile loading and since the pin of the I.F connection is larger than that of the F.H connection and therefore is less likely to have a failure. An additional advantage of the I.F connection is the larger opening force or the amount of external loading that the connection can handle before opening.

\section*{APPENDIX IV}

CALCULATED STRAINS AND DEFLECTIONS OF DRILLING SUBS COMPARED TO EXPERIMENTAL MEASUREMENTS

\title{
CALCUIATED STRAINS AND DEFLECTIONS OF DRILLING SUBS COMPARED TO EXPERIMENTAL MEASUREMENTS
}

Prepared by:
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\section*{Conclusions}
1) The stress concentration factor at the change in section of the drilling subs, obtained from strain gauge measurements under pure axial load, and under pure bending load, should be essentially constant. A large scatter was actually observed in the concentration factor \((+18 \%\) to \(-6 \%\) of the average value). This scatter is attributed to experimental errors which are at present unexplained. This scatter is larger than the differences between the calculated strain values and the experimental measurements.
2) The calculated strain values, based on a drilling sub with a uniform section (5.5 in. O.D. and 4.125 in I.D.) are in reasonable agreement with the strain gage measurements for combined tensile and bending loading when the geometric stress concentration at the change in section of the drilling subs is taken into account (see Table I).
3) The calculated center deflection is in good agreement with the measured deflection when the initial deflection of the test assembly due to its own weight is taken into account (see Table II).
4) The approximation of a uniform section for the drilling subs may be used in analyses for the behavior of the subs in the guide shoe, but account must be taken of the geometric stress concentrations due to the change in cross section at the hubs.
5) A more gradual transition at the change in section would significantly reduce the stress concentration factor and thereby increase the fatigue life of the drilling subs.

\section*{Summary of Results：}

Calculations of the strains and deflections were made for combined tension and bending loads applied to drilling subs in the manner described in the Weatherford！Lamb U．S．，Inc．report，＂Experimental Evaluation of Optimum 5－1／2＂I．F．Connection Design＂，by L．C．Eichberger（March 1978）．

The drilling sub was modelled as（a）a uniform 5.5 in．O．D．\(\times 4.125\) in． I．D．tube，and（b）a tube of the same cross section with 26 in．long＂tool joints＂assumed to be rigid．The behavior of the uniform section tube was found to be in better agreement with the experimental measurements．

The experimental strain measurements under axial load only and bending load only showed a geometric stress concentration to exist at the end of the 44 in．long central section of the drilling subs．The measured values of this stress concentration at the point of maximum stress（gauge location 12）varied from 1.157 to 1.447 with an average value for all tests of 1.23 ．This variation \((+18 \%\) to \(-6 \%\) of the average）is believed to be due to experimental error， since the stress concentration should be constant for pure tensile or bending loading．

Strains were calculated from the analytical treatment of a uniform section tube under combined tension and bending，at the tube center（location of gauge业8），and at the location of gauge 非12．The calculated strains at gauge 婇12 were multiplied by 1.23 to account for the geometric stress concentration． These calculated strains are compared to the measured strains．（for the extreme values of bending load in each combined load test）in Table \(I\) ．

The total deflection of the center of the assembly under combined loading was calculated and found to be substantially less than the measured values listed in Tables Cl－C4 of the Weatherford／Lamb report（for combined loading）．

This is attributed to the omission of the initial deflection due to the weight of the drilling subs and the weight of the loading beam. The dial gauge readings were most probably zeroed prior to the application of the axial (or the bending) load, and the initial deflection must therefore be added to the dial gauge readings to give a comparison with the calculated deflections from an initially straight configuration.

The system weights were estimated, and an initial center deflection of 0.481 was calculated. The measured center deflection, plus 0.481 in., is compared to the calculated center deflection of the uniform tube under combined loading in Table II.

The calculated and measured bending deflections over the central portion of the test assembly are compared in Table III.

The Weatherford/Lamb report states that a bending load of 951891 in .1 b . in combination with a 402025 lb . tension produces a curvature of \(16^{\circ} / 100 \mathrm{ft}\). The slope of the drilling sub at two adjacent hubs was not measured, so it is unclear how this curvature was measured. The slope change was calculated to be \(17.0^{\circ} / 100 \mathrm{ft}\). (hub-to-hub) under this combination of loads.

The analysis of the behavior of the drilling subs under combined loading is given in the appendix.

TABLE I

Calculated and Measured Strain Values at Gauges 8 and 12
Under Combined Loading ( \(\times 10^{-6} \mathrm{in}\)./in.)
\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|c|}
\hline & & & & & & Gauge 8 & & & uge 12 & \\
\hline &  & \[
\begin{gathered}
\# \\
\text { Page } \\
\hline
\end{gathered}
\] & \[
\begin{array}{r}
\text { Bend. Load. } \\
\text { in. } 1 \mathrm{~b}_{\mathrm{C}} \\
\hline
\end{array}
\] & Gauges & Calculated & Measured & \% Diff. & Calculated* & Measured & \% Diff. \\
\hline & A4a & A16 & 827992 & Odd & 748 & 655 & -12 & 859 & 838 & -2 \\
\hline & A4b & A20 & 827992 & Even & 1830 & 1801 & -2 & 2313 & 2583 & +12 \\
\hline \(\stackrel{1}{\sim}\) & A8a & A40 & 951891 & Odd & 667 & 628 & -6 & 750 & 698 & -7 \\
\hline & A8b & A44 & 951891 & Even & 1912 & 1922 & +0.5 & 2421 & 2551 & +5 \\
\hline & A12a & A 64 & 920916 & Odd & 687 & 615 & -10 & 777 & 786 & +1 \\
\hline & A12b & A 68 & 920916 & Even & 1891 & 1913 & +1 & 2394 & 2782 & +16 \\
\hline & A16a & A88 & 941566 & Odd & 674 & 644 & -4 & 759 & 820 & +8 \\
\hline & A16b & A 92 & 941566 & Even & 1905 & 1929 & +1 & 2412 & 2800 & +16 \\
\hline
\end{tabular}
* Velues calculated for a uniform section were increased by 1.23 times to account for the geometric stress concentration.
\# From Reference 5
```

Calculated and Measured Values of Total Center Deflection
Under Combined Loads

```
\begin{tabular}{|c|c|c|c|c|c|}
\hline \[
\begin{gathered}
\# \\
\text { Table } \\
\hline
\end{gathered}
\] & \[
\begin{gathered}
\# \\
\text { Page } \\
\hline
\end{gathered}
\] & Bending Load, in. 1 b . & \[
\begin{aligned}
& \text { Deflect } \\
& \text { Calculated }
\end{aligned}
\] & \begin{tabular}{l}
\(s\), in. \\
Measured \({ }^{*}\)
\end{tabular} & \% Difference \\
\hline C1 & C2 & 827992 & 1.624 & 1.613 & -0.7 \\
\hline C2 & C2 & 951891 & 1.867 & 1.775 & -5.2 \\
\hline C3 & C3 & 920916 & 1.806 & 1.788 & -1.0 \\
\hline C4 & C3 & 941566 & 1.846 & 1.793 & -3.0 \\
\hline
\end{tabular}


(2) MUMERICAL VALJES-FLEXIBLE, UUIFORM
\[
T=40202516 .
\]
\[
a=42.125
\]
\[
b=130.5
\]
H.p.
\[
\begin{aligned}
& b=130.5 \\
& E I=805 \times 10^{8} 13 \mathrm{sin}^{2}
\end{aligned}
\]
(1) \(\alpha=2.1245 \times 10^{-2}\)
\[
\alpha^{2}=4.5148 \times 10^{-3}
\]
(1) \(\alpha a=0.895072\)
(3) \(\alpha 6=2.121865\)
(5) \(\sinh ^{2} \alpha a=1.019467\)
(5) \(\sin \alpha b=7.97015 \%\)
(6)
\[
\begin{aligned}
& \cosh \alpha a=1.428045 \\
& \cosh \alpha 5=8.033449
\end{aligned}
\]

QQ. 8
\[
F=-\frac{\sinh \alpha b}{\cosh \alpha 6} E=-\overbrace{-.9922=}^{(8)} E
\]
Q.7 \(B \cosh \alpha a=E(\sinh \alpha \varepsilon-.99222 \cosh \alpha \varepsilon)=-.39741 E\)
\[
\begin{aligned}
& E=-3.582829 \mathrm{~B} \\
& F=3.567884 \mathrm{~B}
\end{aligned}
\]
0.6
\[
\begin{aligned}
& \alpha B\left(\sinh \alpha a-\frac{E}{B} \cos n d a-\frac{G}{B} \sin \alpha a\right)=G \\
& G=0.053458 B
\end{aligned}
\]
2.5
\[
\begin{aligned}
H & =B\left(\operatorname{cosin} 2 l a-1-\frac{E}{B} \sin 2 a-\frac{F}{B} \cos 2 a-\frac{G}{B} a\right) \\
& =-3.251915 B
\end{aligned}
\]

Ea. \(9^{\prime}\)
\[
\begin{gathered}
\left(1+\frac{G}{B} b+\frac{H}{B}\right) B=\frac{F_{0}}{T}(b-a) \\
4.724351 B=88.375 \frac{F_{0}}{T} \\
\text { (Hacted) } B=18.763 \frac{F_{0}}{T}
\end{gathered}
\]
or
\[
\begin{array}{cc}
B=0.211669 & \frac{\text { Bato. Mом }}{T} \\
B=5.2651 \times 10^{-7} & \begin{array}{c}
\text { (B0x10. Mon. }) \\
\text { in. } 1 \mathrm{~b} .
\end{array}
\end{array}
\]
3.
5. \begin{tabular}{l|l|l|l|}
\hline
\end{tabular} , CONSIDER HUBS RIGID

\(x=0\) :
\[
\begin{aligned}
& y(0)=0 \\
& 4^{\prime}(0)=0 \\
& 4^{\prime \prime}(0)=M_{0} / E_{I} \\
& y^{\prime \prime \prime}(0)=0
\end{aligned}
\]
\[
\begin{aligned}
& a=22 \\
& b=42.125 \\
& c=48 \\
& d=92 \\
& a=130.5
\end{aligned}
\]

\[
\Sigma M_{a}=0:
\]
\[
E I_{4}(a)+F_{0}(b-a)+T(y(c)-y(a))=
\]
\[
F(c-a)+E I y^{\prime \prime}(c)
\]
\[
E I\left(y^{\prime \prime}(a)-y^{\prime \prime}(c)\right)+T(y(c)-y(a))=F_{0}(c-b)
\]
\(2 \leqslant \cos B 2:\)

\(T_{y}(d)+M_{0}=F_{0}(d-b)+\underset{-151-}{E I} y^{\prime \prime}(d){ }^{d}\)
\[
\begin{aligned}
& \varepsilon I y^{\prime \prime}(d)+T y^{\prime}(d)(e-d)=F_{0}(\varepsilon-d) \\
& \sum M_{0}=0:
\end{aligned}
\]
4).
\(0 \leqslant x \leqslant a\) 1. \(\alpha^{2}=\frac{T}{E x}, E I=\frac{T}{\alpha^{2}}\)
\[
\begin{aligned}
& y=A \sinh \alpha x+B \cosh \alpha x+C x+D \\
& y^{\prime}=A \alpha \cosh \alpha x+B \alpha \sinh \alpha x+C \\
& y^{\prime \prime}=\alpha^{2}(A \sinh \alpha x+B \cosh \alpha x) \\
& y^{\prime \prime}=\alpha^{3}(A \cosh \alpha x+B \sinh \alpha x) \\
& C \leq x \leq d
\end{aligned}
\]
\[
\begin{aligned}
& y^{\prime}=E \sinh \alpha x+F \cosh \alpha x+G x+\angle 1 \\
& y^{\prime}=E \alpha \cosh \alpha x+F \alpha \sinh \alpha x+G \\
& y^{\prime \prime}=\alpha^{2} f(E \sinh \alpha x+F(\cosh \alpha x)
\end{aligned}
\]
7): \(y^{\prime \prime \prime}(0)=0=A \alpha^{3} \Rightarrow A=0\)
2) \(y^{\prime}(0)=0=c \Rightarrow c=0\)
1) \(y(0)=0 \Rightarrow y=B(\cosh \alpha x-1)\)
\[
\left.\begin{array}{l}
y^{\prime}=B \alpha \sinh \alpha x \\
y^{\prime \prime}=B \alpha^{2} \cosh \alpha x
\end{array}\right\} \quad 0 \leqslant x \leqslant a
\]
3) \(y^{\prime \prime}(0)=\mu_{0} / E I \Rightarrow \mu_{0}=B T\)
5) \(B \alpha \sinh \alpha \alpha=E \alpha \cosh \alpha c+F \alpha \sinh \alpha c+G\).
b) Esinh \(\alpha c+F\) cesh \(\alpha c+G c+H=B(\tanh \alpha a-1)+(B \alpha \sinh \alpha a)(c-a)\) \(E \sinh \alpha c+F \cosh \alpha c+G c+H=B(\cosh \alpha a+(c-a) d \sinh \alpha a-1)\)
p) \(\frac{T}{\alpha^{2}}\left(y^{\prime \prime}(a)-y^{\prime \prime}(c)\right)+T(y(c)-y(a))=F_{0}(c-b)\)
on usines \(c\left(y(c)-y(a)=y^{\prime}(a)(c-a)\right.\)
\[
B \cosh \alpha a-\varepsilon \operatorname{senh} \alpha c-F \cosh \alpha c+y(c)-y(a)=\frac{F_{0}(c-1)}{T}
\]
os
\[
G c+H+B=\frac{F_{0}(c-b)}{T}
\]
\[
\begin{aligned}
& B \cosh \alpha a-E \sin h \alpha c-T \cosh \alpha c+E \sin \alpha \alpha c+F \cosh \alpha c+G c+11 \\
& -B(\cosh +a-1)=\frac{F_{-}(c-b)}{7}
\end{aligned}
\]
8) \(T(E \sinh \alpha d+F \cosh \alpha d)+T(E-d)(E \alpha \cosh \alpha \beta+F \alpha \sinh \alpha d+G)\)
\[
=F_{0}(e-d)
\]
on
\(8^{\prime \prime} E(\sinh \alpha d=(2-d) \alpha \cosh \alpha d]+F[\cosh \alpha d+(e-d) \alpha \sin \alpha d]\)
\[
\rightarrow(e-d) G=F_{0}(e-d) / T
\]
9) \(\quad y(d)+B=\frac{F_{0}}{T}(d-b)+\frac{1}{\alpha^{2}} y^{\prime \prime}(d)\)
\(E \sin \alpha d+F \cosh \alpha d+G d+H-E \sin h \alpha d-F \operatorname{sench} \alpha d+B=\frac{F_{0}}{T}(d-b)\) oe
\[
\left.9^{\prime}\right) \quad G d+H+B=\frac{F_{0}(d-b)}{T}
\]

EQUATION SUMENARY ( \(B, E, F, G, H\) UNKNOWRS)
(1) \(B \alpha \sinh \alpha a=E \alpha \cosh \alpha c+F \alpha \sinh \alpha c+G\)
(2) \(B[\cosh \alpha a+(c-a) \alpha \sinh \alpha a-1]=E \sinh \alpha c+f \cosh \alpha c+G c++1\)
(3) \(G C+H+B=F_{0}(c-b) / T\)
(4) \(E[\sinh \alpha d+(e-d) \alpha \cosh \alpha d]+F[\cosh \alpha d+(e-d i \alpha \sin \alpha d]\)
\[
+(e-d) G=F_{0}(e-d) / T
\]
(5) \(\quad G d+H+B=F_{0}(d-6) / T\)

SOLUTRON:
(3), (b) \(\quad G(d-c)=F_{0}(d-c) / T \Rightarrow G_{2}=F_{0} / T\)
(5) \(A+B=-\frac{F_{0} b}{T} \Rightarrow H=-B-\frac{F_{0} b}{T}\)

Dian (2) eccours
\(B[\cosh \alpha a+(c-a) \alpha \sinh \alpha a-i]=E \sinh \alpha c+F \cosh \alpha c+\frac{F_{0}}{T}(c-6)-B\) on
\[
B[\cosh \alpha a+(c-a) \alpha \sinh \alpha a]-E \sinh \alpha c-F \operatorname{cod} \alpha c=\frac{\epsilon_{0}}{T}(c-\infty)
\]
\(\qquad\) \(1 M\) \(\qquad\) \(B, C\)
\[
B \alpha \sinh d a-E d \cosh d c-F \alpha \sinh \alpha c=F_{0} / T
\]
(e) \(B[\cosh \alpha a+(c-a) \alpha \sinh \alpha a]-E \sinh \alpha c-F \cosh \alpha c=\frac{F_{0}}{T}(c-b)\)
(3) \(E[\sinh \alpha d+(e-d) \alpha \cosh \alpha d]+F[\cosh \alpha d+(c-d) \alpha \sinh \alpha d]=0\)
\[
\begin{aligned}
& a=22 \\
& b=42.125 \\
& c=48 \\
& d=92 \\
& e=130.5
\end{aligned}
\]
\[
\begin{aligned}
& T=40202516 . \\
& F_{0}=V_{A R L I A B L E} \\
& \alpha^{2}=4.5148 \times 10^{-4} \\
& \alpha=2.1248 \times 10^{-2}
\end{aligned}
\]
\[
\begin{aligned}
& \sinh \alpha a=0.4847 \\
& \sinh \alpha c=1.201 \\
& \sinh \alpha d=3.4605 \\
& \cosh \alpha a=1.1113 \\
& \cosh \alpha c=1.5668 \\
& \cosh \alpha d=3.6021
\end{aligned}
\]
(1) \(0.010298212 B-0.033290921 E-0.025628264 F=F_{0} / T\)
(2) \(1.379015143 \mathrm{~B}-1.206149496 \mathrm{E}-1.566779055 \mathrm{~F}=5.875 \mathrm{~F}_{0} / \mathrm{T}\) (a.1)
(3)
\[
\begin{gathered}
6.407209180 \sigma_{(2.2)} 6.43297186 \sigma=0 \\
F=-0.995995213 E \\
0.010298221213-0.007765293 E=F_{0} / T \\
1.379015143 \mathrm{~B}+0.354354943 E=5.875 F_{0} / T .
\end{gathered}
\]
\[
\begin{aligned}
3.891621015 \mathrm{~B}+E & =16.57142161 \mathrm{~F} / \mathrm{T} \\
1.326185786 \mathrm{~B}-E & =128.7781414 \mathrm{Fo} / \mathrm{T} \\
5.2178 \mathrm{~B} & =145.357563 \mathrm{~F} / \mathrm{T}
\end{aligned}
\]
(CHTCK00)
\[
B=27.858
\]
\(\begin{aligned} &\because 7) \text { DHFLCTTOUS } \\ & \text { FCLXIBLE, UNIGORNS. }\end{aligned}\)
\[
\begin{aligned}
& y(42.125 \\
& y(130.5)=E .007 F_{0} / T=B(\cosh \alpha a-1) \\
& y+6+F \cosh +6+G 6+H=69.67 \mathrm{~F} / \mathrm{F} / \mathrm{T}
\end{aligned}
\]

RIGID HUBS
\[
\begin{aligned}
& y(42.125)=y(22)+y^{\prime}(2 x)(20.125)=8.874 \mathrm{Fo} / \mathrm{T} \\
& y(130.5)=60.467 \mathrm{~F} / \mathrm{T}
\end{aligned}
\]

SS2DD. Asen \(=F_{0}(130.5-42.125)=88.375 F_{0}\)
\[
\begin{aligned}
& \begin{array}{l}
T=402025, \frac{F_{0}}{T}=\frac{80210.210}{(87.375)(d} \\
y(42.125)=2.254 \times 10^{-7} \text { (3NuD.21.) }
\end{array} \\
& 7 \text { ) })_{y}(130.5)=1.761 \times 10^{-6} \text { (BSND. M.) } \\
& \text { FLEx, vulforel }
\end{aligned}
\]

RIGID AUBS
\[
\begin{aligned}
& y(42.125)=2.498 \times 10^{-7} \text { (BAND. M.) } \\
& y(130.5)=1.702910^{-6} \text { (BEND.M.) }
\end{aligned}
\]

SAO chere: \(C 2 \quad B M=827992, C=1.132\)
\[
\begin{aligned}
\text { yflax } & =1.624 \\
\text { 4rigid } & =1.41 \\
\text { BM } & =920916, C=1.307 \\
& \text { 4flax }
\end{aligned}=1.806
\]

DIAL GAGE READIRIGS ARE CHANGE IN DSEL. FROMINITALL CURVE OF DEFLECTION DUE TO PIRE WERAHT. ESTIUATE inITAL DEFLECTION!
8)

DETELOCTION aftal.


COUTGR DEFCECTION \(\omega / R\) To GUDS
\[
\begin{aligned}
\delta_{1}=\frac{5}{24 E I} \ell^{4} & \text { (Due To } 5.5^{*} 0.0 . \times 4.125 \text { I.0. sT22 ) } \\
& \omega=\frac{(2.9)\left(5.5^{2}-4.125^{2}\right) \pi(62.4)}{2(1728)} \cong 4 \mathrm{~F} / 14 \\
I I & =8.905 \times 10^{8} \mathrm{in}^{2} / 6 \\
l & =130.5 \mathrm{i}
\end{aligned}
\]
\[
\delta_{1}=0.256^{\circ}
\]
\(\delta_{2}=\) DEFLETION DUE TO HWB WDGIATA LOADIMG
BEACH WEIGAT

LIUB : \(7^{\prime \prime} 0.0 . \times 5.5\) I. 0. \(\times 26^{\prime \prime}\)
\[
W_{h}=\frac{\left(49-5.5^{2}\right)(7.9)(63.4)(26) \pi}{4 \cdot 1728} \cong 11016
\]

\[
\begin{aligned}
& w_{b}=\frac{3 \times 8 \times \frac{1}{3} \times 74.35 \times 7.9 \times 62.4 \times \pi}{4 \times 1728} \cong 100 \mathrm{lb} \\
& w_{\text {LOAD sTeAP }} \cong 50 / \mathrm{h} \\
& w_{\text {SACK }}
\end{aligned}
\]
\[
W=W_{h}+W_{0}+W_{\text {Lers stery }}+W_{\text {JACK }} \cong 300 \mathrm{lb} .
\]

9)
\[
\begin{aligned}
& S_{2}=\frac{W}{2 E I}\left(\frac{2}{3} l^{3}-l a^{2}+\frac{a^{3}}{3}\right) \quad a=35, l=130.5, E Z=8.905 \times 10^{8} \\
& S_{2}=0.225 \\
& S=\text { IUITTA MID-HOIMT DEFCECTION }=\sigma_{1}+S_{2}=0.481 \mathrm{in} .
\end{aligned}
\]

ANB - TO-HUB SCOPG CHANEE
\(y^{\prime}=B \alpha \sinh \alpha x, y^{\prime}(35)=9.108\left(x 10^{-9}(B\right.\) BNeD \(\cos 0)\) EADMers \(=5.2186 \times 10^{-3}\) (B...) 08 a \(/ 35\) inches whech aivrs \(1.7892 \times 10^{-5}\) (8SuD. LOAD) \(0 / 100 \mathrm{ft}\). on \(17.0^{\circ} / 100^{\circ}\) at sane LOAD- 951891 in. 15 .

CALCULATED STEAIUS
\[
\begin{aligned}
& e_{\text {TBUSBCE } \angle O A D}=\frac{T}{A E}=\frac{402025}{\left.(\pi / 4) / 5.5^{n}-4.125^{2} 3\right) 30 \times 10^{6}}=1288 \mu \mathrm{in/in} . \\
& \left|\epsilon_{\text {BOJD }}\right|=\frac{r d \theta}{d s}=\frac{M r}{E I} \\
& 0 \leqslant x \leqslant a,\left|\epsilon_{3 N 10}\right|=B \alpha^{2} r \cosh \alpha x, r=2.75^{\prime \prime} \\
& \epsilon_{\text {qxial }}=1289 \pm \beta \alpha^{2} r \cosh \alpha x \\
& =1289 \pm 6.537 \times 10^{-4} \text { (BovD. LOAD) } \cosh \alpha x
\end{aligned}
\]
\(\left(E_{\text {axia1 }}\right)_{\text {GAGE } 8, x=0}=1.259 \pm 6.537 \times 10^{-4}\) (3ones. \(\operatorname{LOE0)}\)
\(\left(\epsilon_{\text {axial }}\right)_{\text {GHaE } 12, x=20^{\prime \prime}}=\left[1289 \pm 7.1366 \times 10^{-4}\right.\) (S3xDD. COAD \(\left.)\right](1.23)\)
(ASSURIMG THE ALONEE MEASURED STNESS CONCENTINATIOX)
BaIDCLL LOAD \(=F_{0}(e-b)=88.375 F_{0}\) IS CISTEO IN TASULAN OATA OF WEATHERFDRD / LAMB REPORT
 Men porut w/e ouns (ser g. 7)

MIDDCE SUB DODEGCTOUS (IMITIAC), AT \(x=12, x=34 . \frac{1}{5} 12\)
\(0 \leq x \leq a\)
\[
\begin{aligned}
& E I y_{2}^{\prime \prime}=W(l-a) \quad E I y_{2}^{\prime}=W(l-a) x \\
& E I y_{2}=W(l-a) \frac{x^{2}}{2}
\end{aligned}
\]
\[
y_{2}=\frac{W}{E I}(2-a) \frac{x^{2}}{2}
\]
\[
y_{1}+y_{2}=\text { IMITAL DFFESTROR }
\]
H.P.
\[
\begin{aligned}
& w=4 \# / \mathrm{in} \\
& \text { 1.p. } \quad W=300=4 \\
& 0 \\
& 1 \quad l=8.905 \times 10^{8} \mathrm{in}^{2} / \mathrm{g} \\
& l=(30.5 \mathrm{in} \\
& a=35 \mathrm{im} \\
& l-a=95.5 \mathrm{in} . \\
& x
\end{aligned}
\]
\[
\frac{x=12}{y_{1}+y_{2}=0.0028+0.0023=.0051}
\]
\[
\frac{x=34.812}{y_{1}+y_{2}=.022 y}+.0195=.0424
\]
\[
\begin{aligned}
& M_{0}<L_{1}^{L L C L} \\
& M_{0}=\omega L^{2}-(\omega l) \frac{l}{2}=\frac{\omega l^{2}}{2} \\
& \text { EI } y_{1}^{\prime \prime}=\frac{\omega l^{2}}{2}-\frac{\omega x^{2}}{2}=\frac{\omega}{2}\left(l^{2}-x^{2}\right) \\
& \text { EI } y_{1}^{\prime}=\frac{w}{2}\left(Q^{2} x-\frac{x^{3}}{3}\right)+t_{1}^{7} 0 \\
& E I_{y}=\frac{u}{2}\left(e^{2} \frac{x^{2}}{2}-\frac{x^{4}}{12}\right) \Rightarrow y_{1}=\frac{u}{\Delta r E I}\left(e^{2} x^{2}-\frac{x^{4}}{6}\right)
\end{aligned}
\]

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